

# Exchange coupling in selected Eu compounds


Jan Kunes  
UC Davis



# Collaborations

- Warren E. Pickett, UC Davis
- Wei Ku, LBNL
- Robert Laskowski, Uni. Aarhus
- Pavel Novak, IoF Prague

# Outline

- Rare earth materials
  - Basics of LDA+U
  - EuX - ferromagnetic insulators
  - Bcc Eu - spin spiral groundstate
  - EuB<sub>6</sub> - semimetal?
  - Summary
- 

# Physics of 4f electrons

- Localized 4f shell - interactions: Coulomb repulsion, spin-orbit coupling, hopping (hybridization)
- Phenomena: localization-delocalization ( $\alpha - \gamma$  Cerium), valence fluctuation, various types of magnetic ordering
- Anderson lattice model



# LDA+U method

Motivation:

Treat on-site interactions explicitly because we do not know how to guess appropriate density functional.

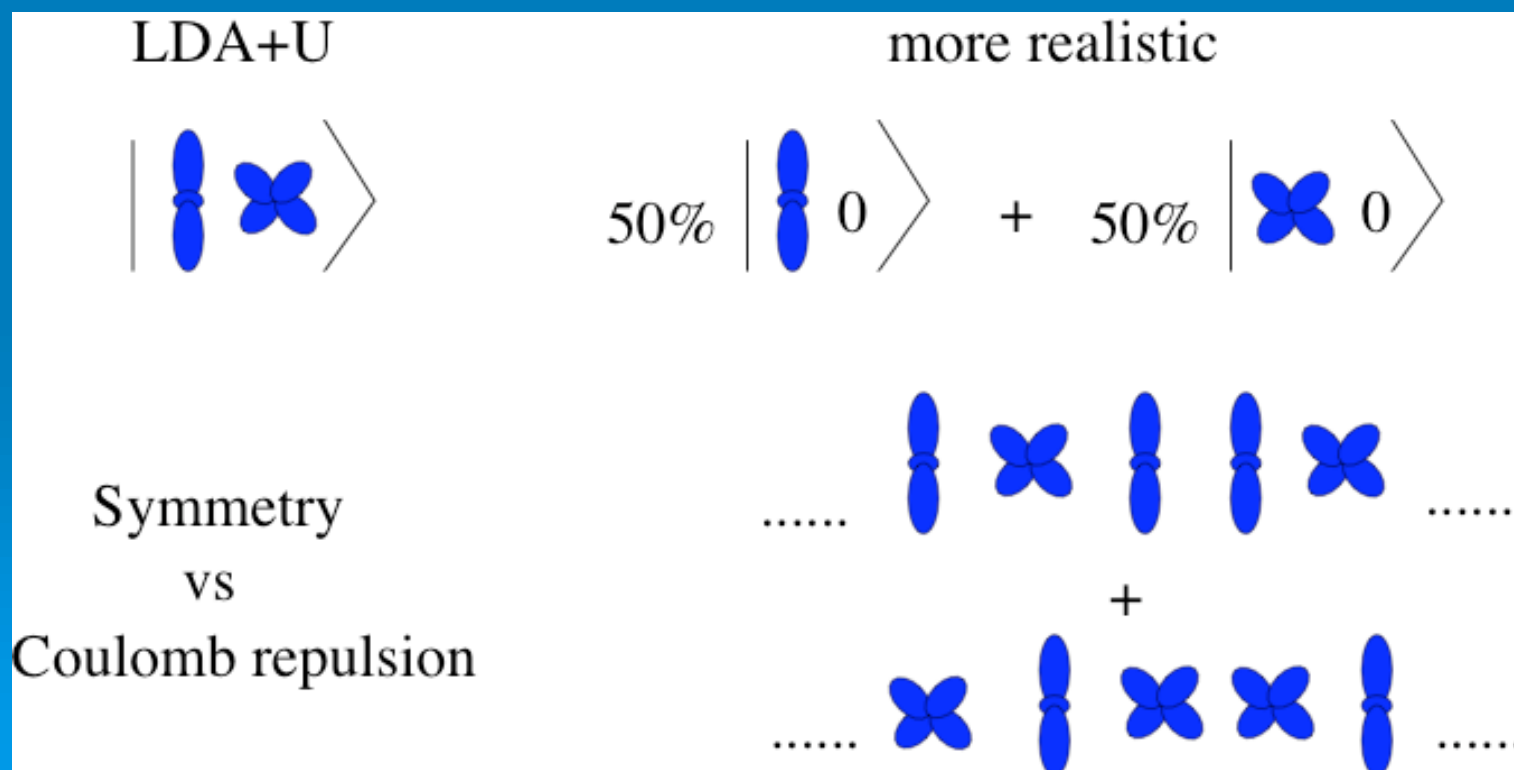
Energy functional:  $E[\rho] = E_{LDA}[\rho] + E_U[n_i(\rho)] - E_{DC}[n_i(\rho)]$

Effective Hamiltonian:  $H = H_0 + H_U(\langle n_i \rangle)$

$H_U$  has a form of effective crystal field

- LDA+U only reasonable for Mott insulator
- Cannot describe local statistical averages - overestimates ordering

Example: 2 equivalent orbitals & 1 electron



# Eu chalcogenides

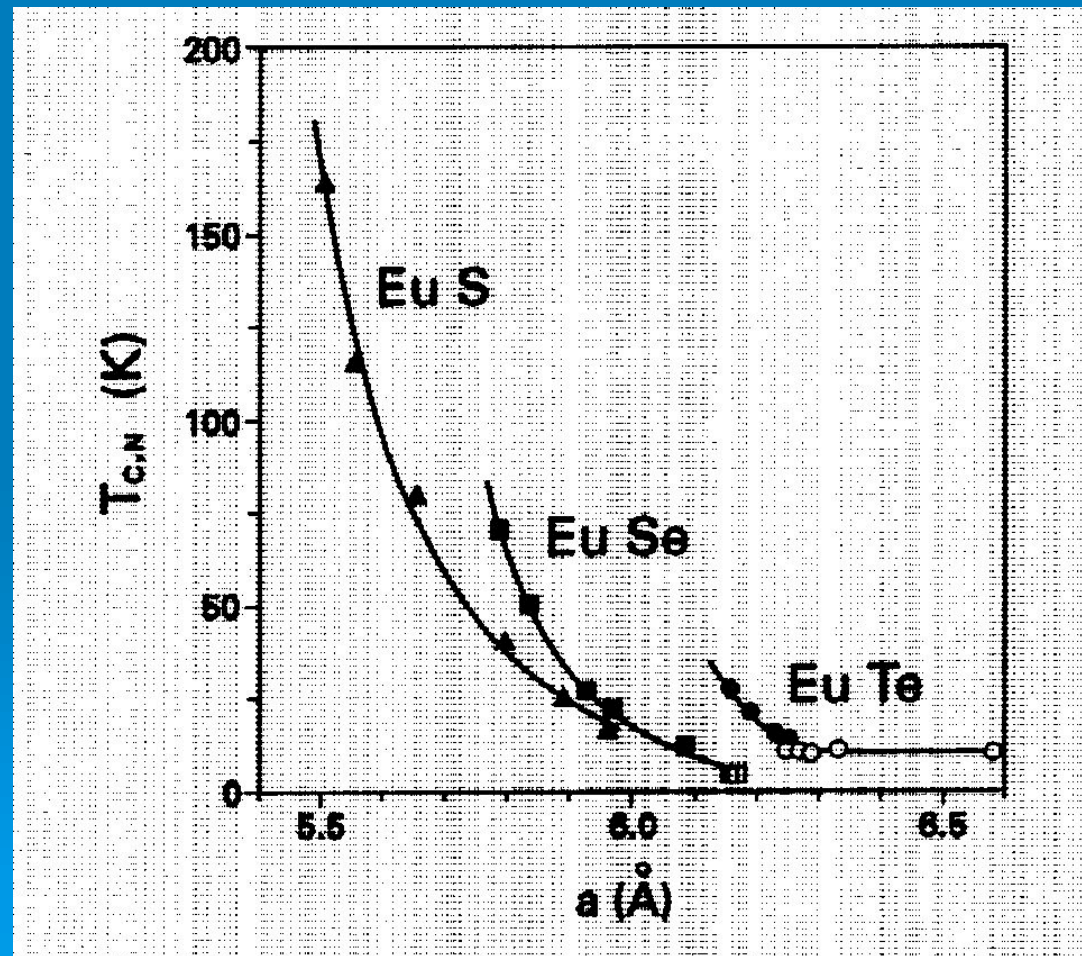
- $\text{Eu}^{2+}$  valency =  $f^7$  configuration
- $\text{NaCl} \rightarrow \text{CsCl}$  (at 12 - 20 GPa)
- $\text{EuO}$  and  $\text{EuS}$  - FM at ambient pressure ( $T_c=68$  K and 16 K)
- $\text{EuSe}$  and  $\text{EuTe}$  - type II AFM at ambient pressure, FM at elevated pressure ( $\sim 10$  GPa)

Quantitative calculation of coupling parameters as a function of pressure.

Important coupling processes?

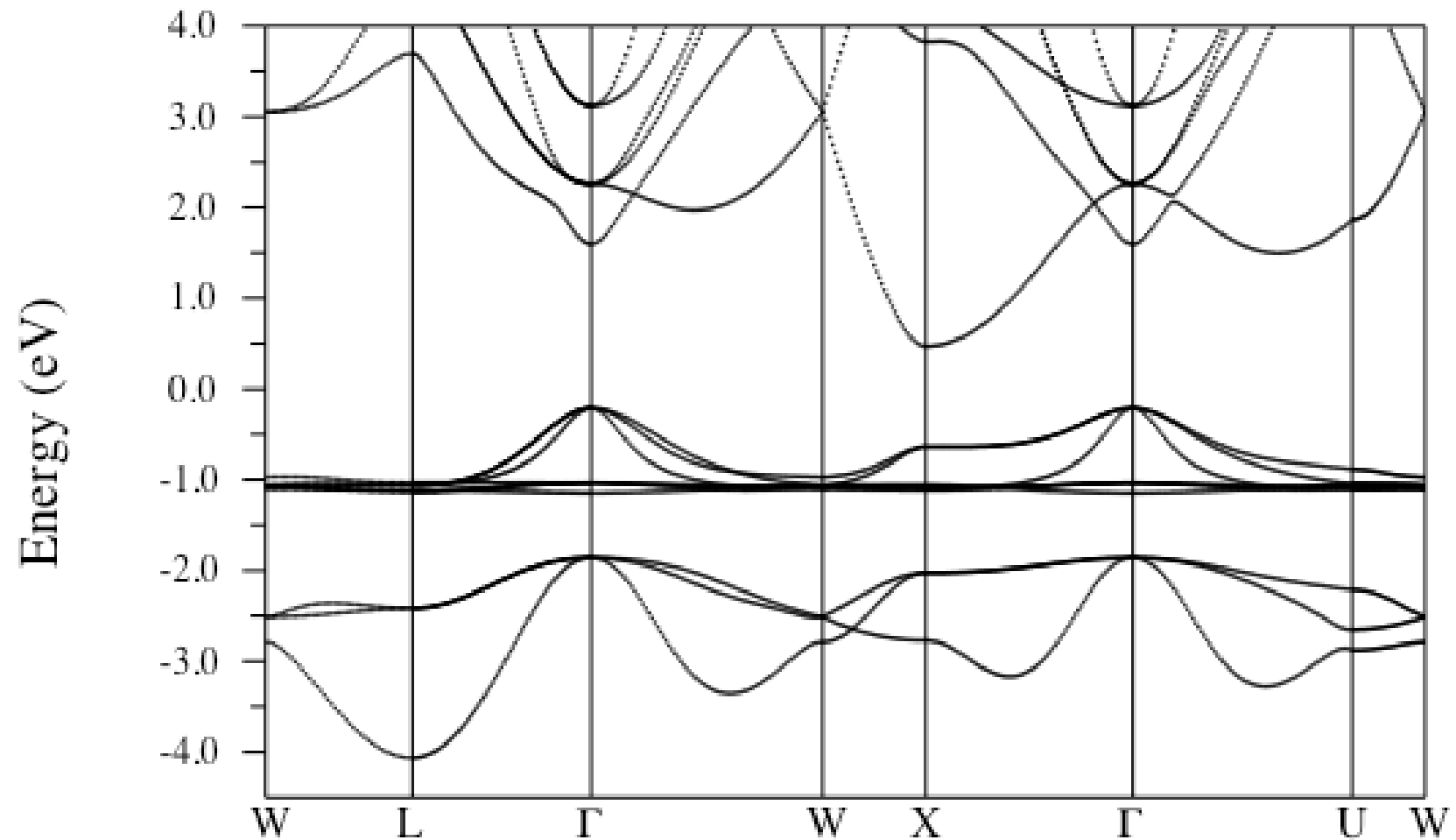
# Effect of Pressure

Goncharenko and Mirebeau, PRL **80** 1082 (1998):



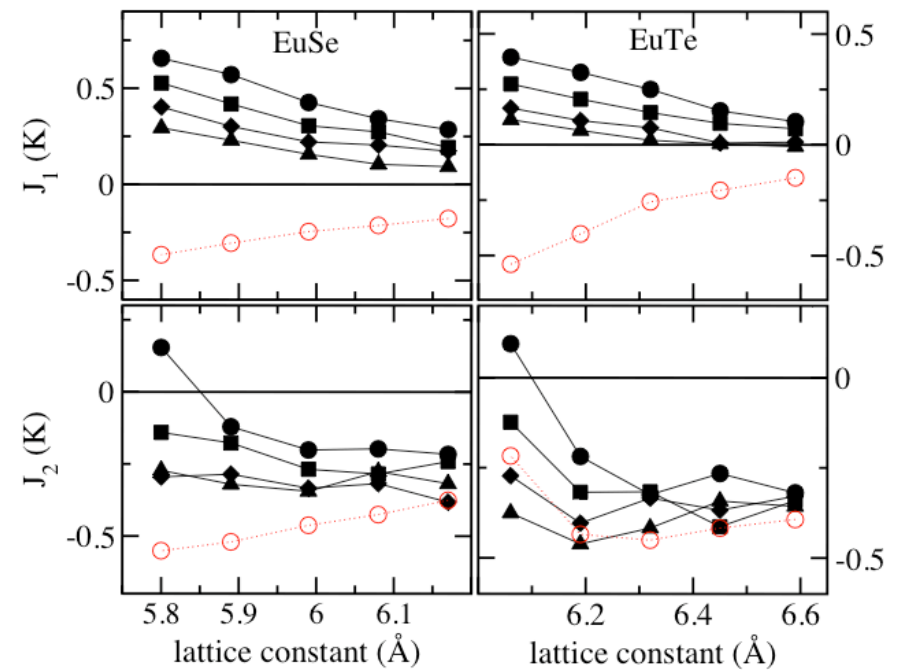
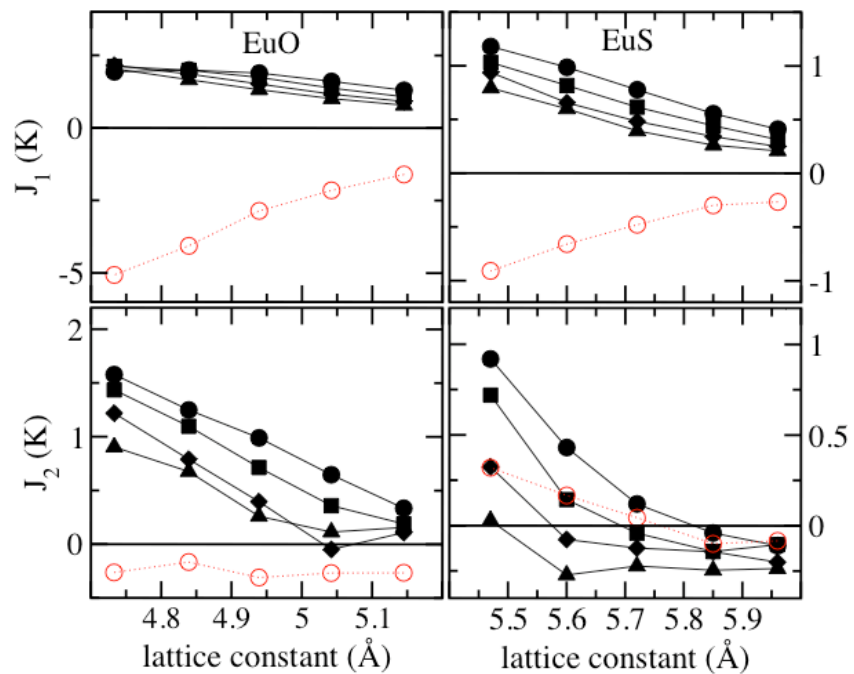


# Band structure



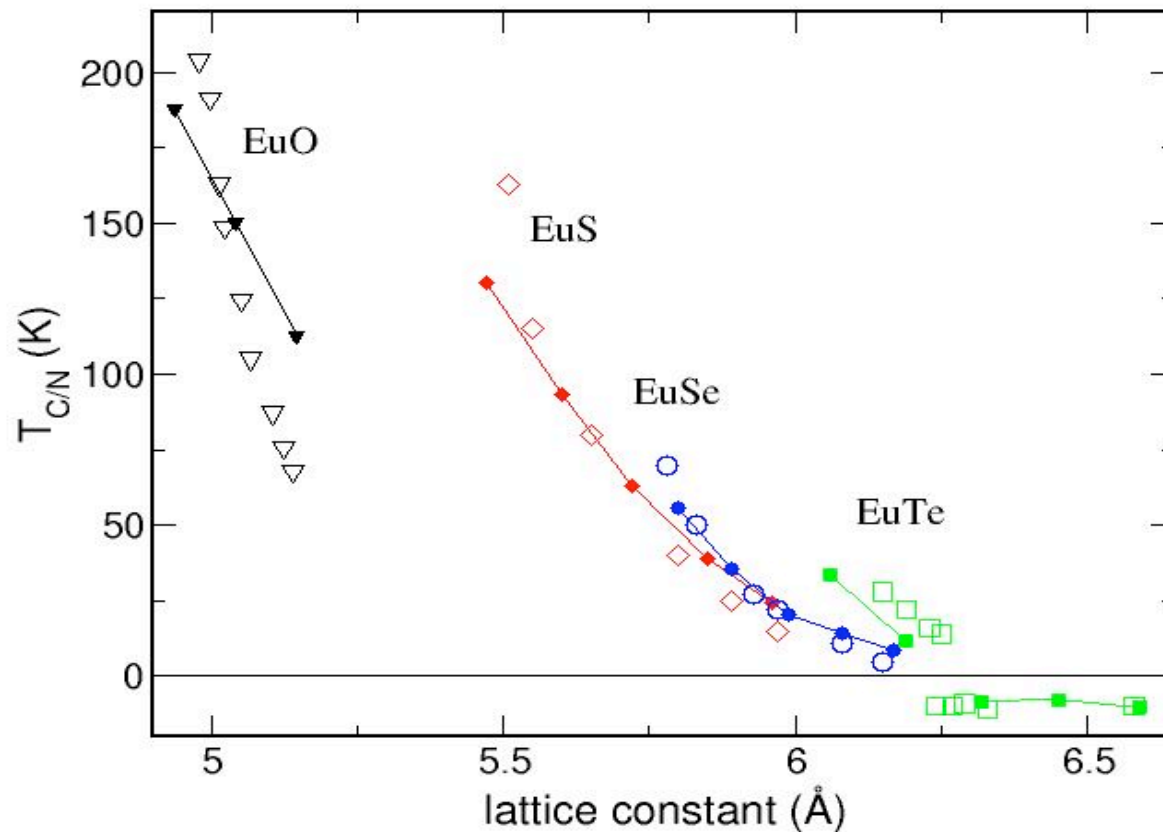
# Effective exchange $J_1$ - $J_2$

$$H = \frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$



# Ordering temperature

$$(k_B T_C)^{-1} = \frac{3}{2S(S+1)} \frac{1}{N} \sum_{\mathbf{q}} [J(\mathbf{0}) - J(\mathbf{q})]^{-1}$$



# LDA+U vs open core

LDA+U

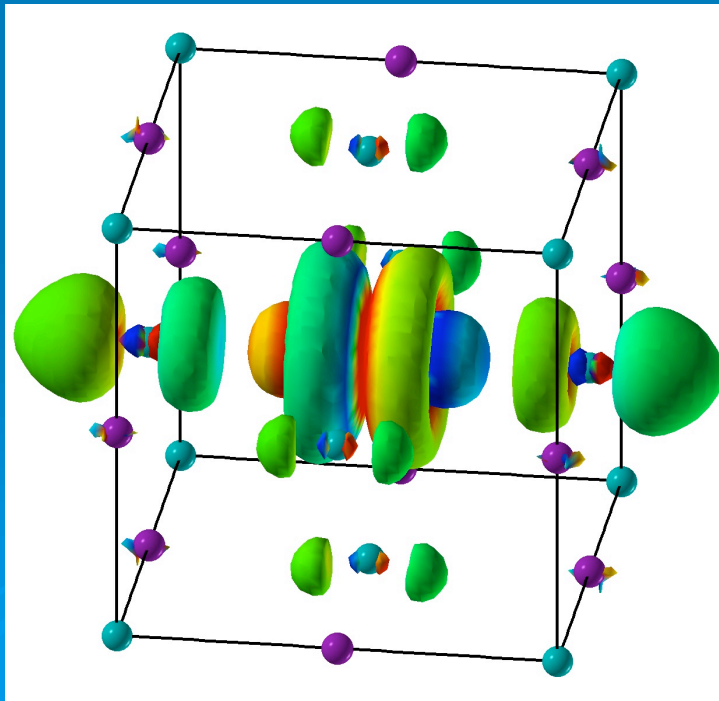
mixing + potential

all exchange processes

open core

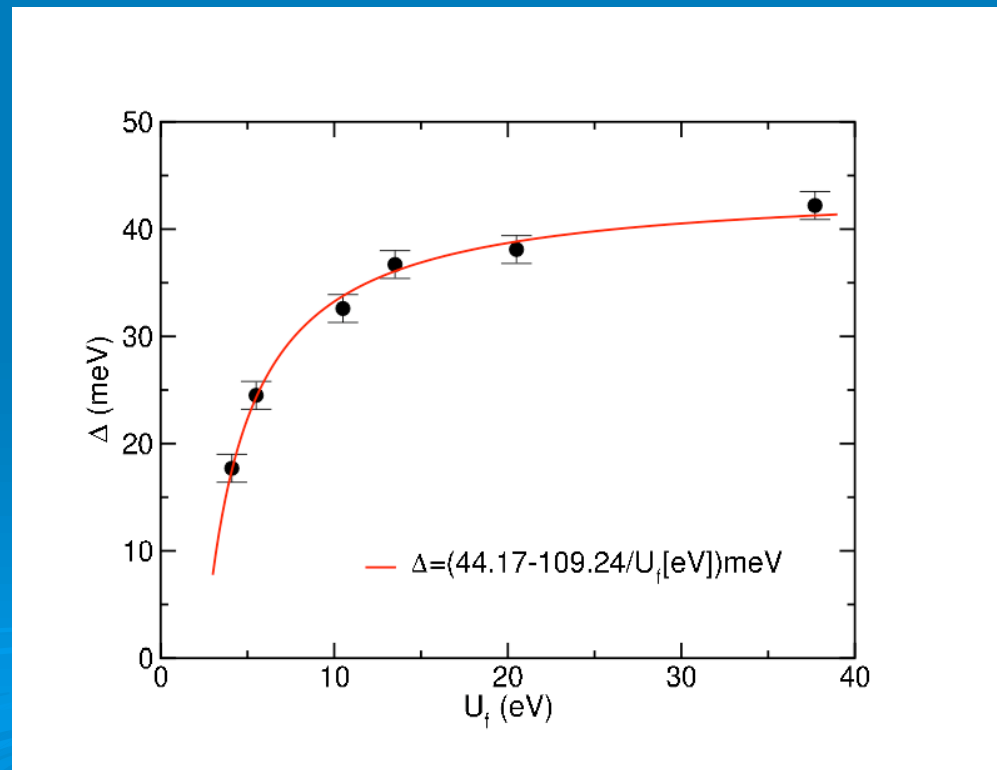
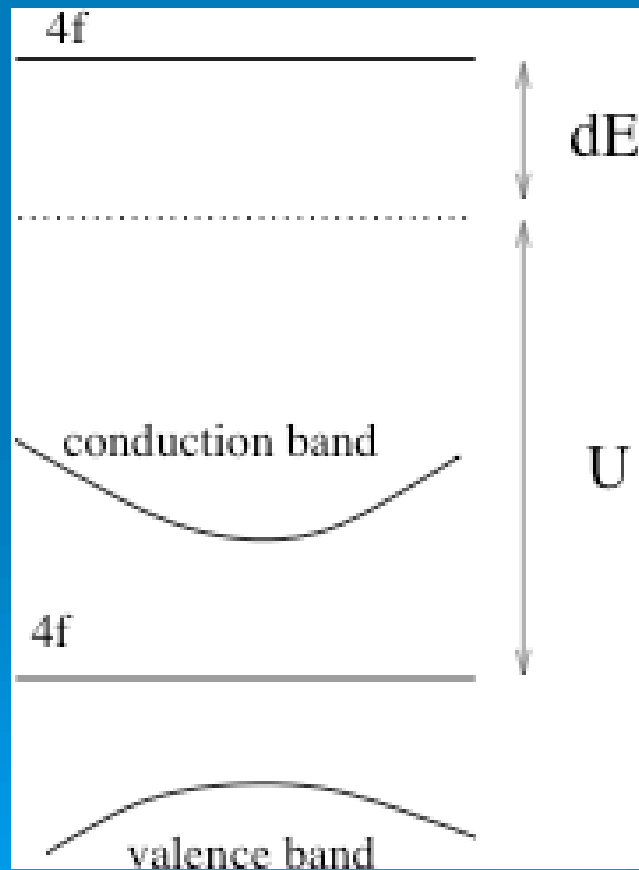
potential only

$J_{f-s_d}$



# f-f super exchange

$$J_{se} \sim 1/U_{eff}$$

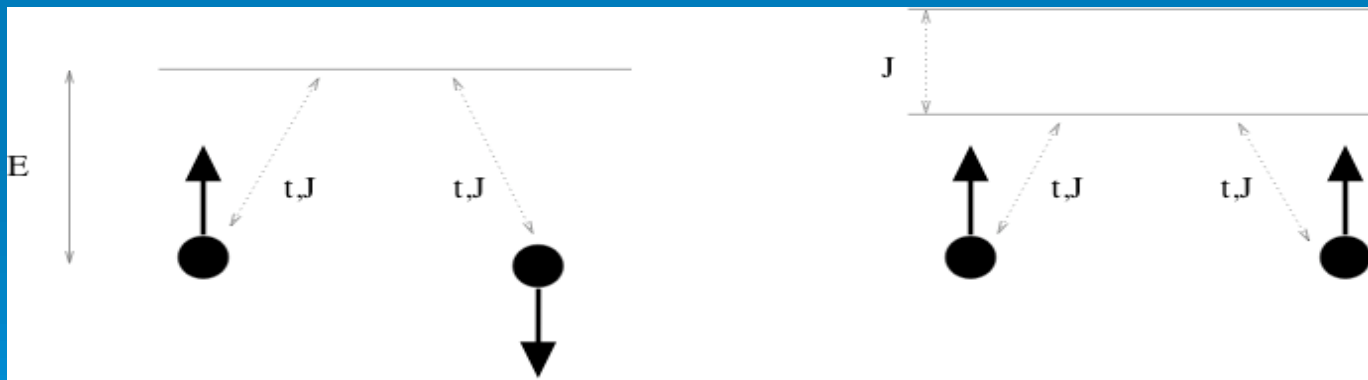


# f-d exchange model

Full diagonalization vs mean field

3-site model:  $U_f$ - infinite, 2 electrons

$$H = E \sum_{\sigma} d_{\sigma}^{\dagger} d_{\sigma} + t \sum_{\sigma, i} (f_{i\sigma}^{\dagger} d_{\sigma} + h.c.) - J \sum_i \mathbf{S}_{f_i} \cdot \mathbf{S}_d$$



$$E_{\uparrow\uparrow} - E_{\uparrow\downarrow} \approx -8 \left( \frac{t}{E} \right)^2 J$$

# EuX - summary

- LDA+U provides reasonable quantitative description of coupling parameters and  $T_C$
- $J_1(p)$  and  $J_2(p)$  follow different pressure dependencies
- Hopping from/to f states is crucial for ferromagnetism
- Unoccupied f bands play active role (f-f super exchange)

# Bcc Eu

- Local moment metal ( $f^7$ )
- Magnetically ordered below  $T_N=90.5$  K
- Spin spiral ground state:  $q_0 \parallel c$ ; pitch of  $48^\circ$  per layer

Magnetic interactions (RKKY)?

Quantitative evaluation of  $T_N$  and  $q_0$  ?

Origin of the spin-spiral ground state?

Computational approaches:

real space vs reciprocal space (spin spirals)



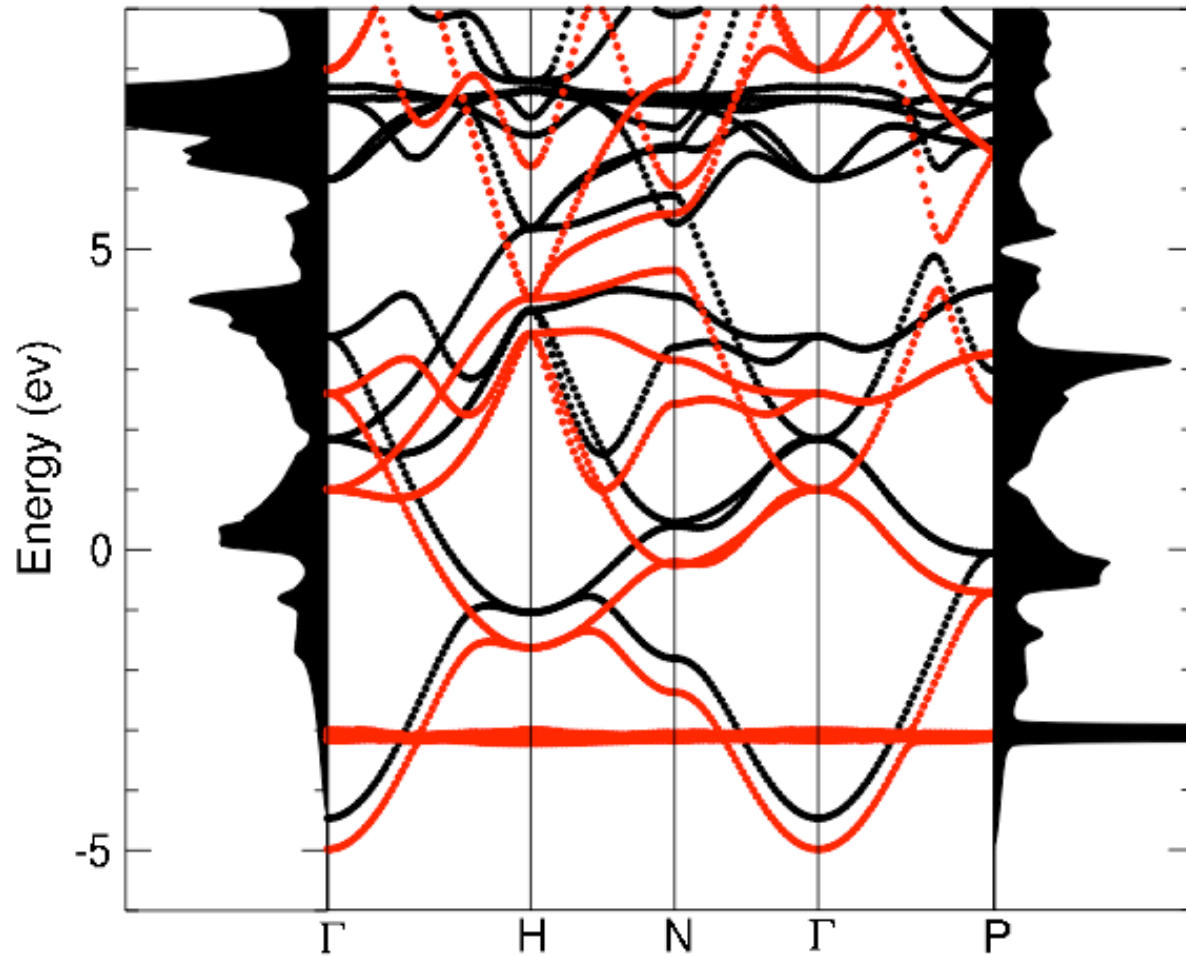
# Spin spirals

$$\mathbf{M}(\mathbf{r}) = (\cos(\mathbf{R} \cdot \mathbf{q}) \sin \Theta, \sin(\mathbf{R} \cdot \mathbf{q}) \sin \Theta, \cos \Theta)$$

- Spin-orbit coupling neglected
- Symmetry operations: lattice translations coupled to spin rotations
- Generalized Bloch theorem:

$$\psi_{\mathbf{k},\mathbf{q}}(\mathbf{r}) = \begin{pmatrix} e^{i(\mathbf{k}+\mathbf{q}/2)\cdot\mathbf{r}} f(\mathbf{r}) \\ e^{i(\mathbf{k}-\mathbf{q}/2)\cdot\mathbf{r}} g(\mathbf{r}) \end{pmatrix}$$

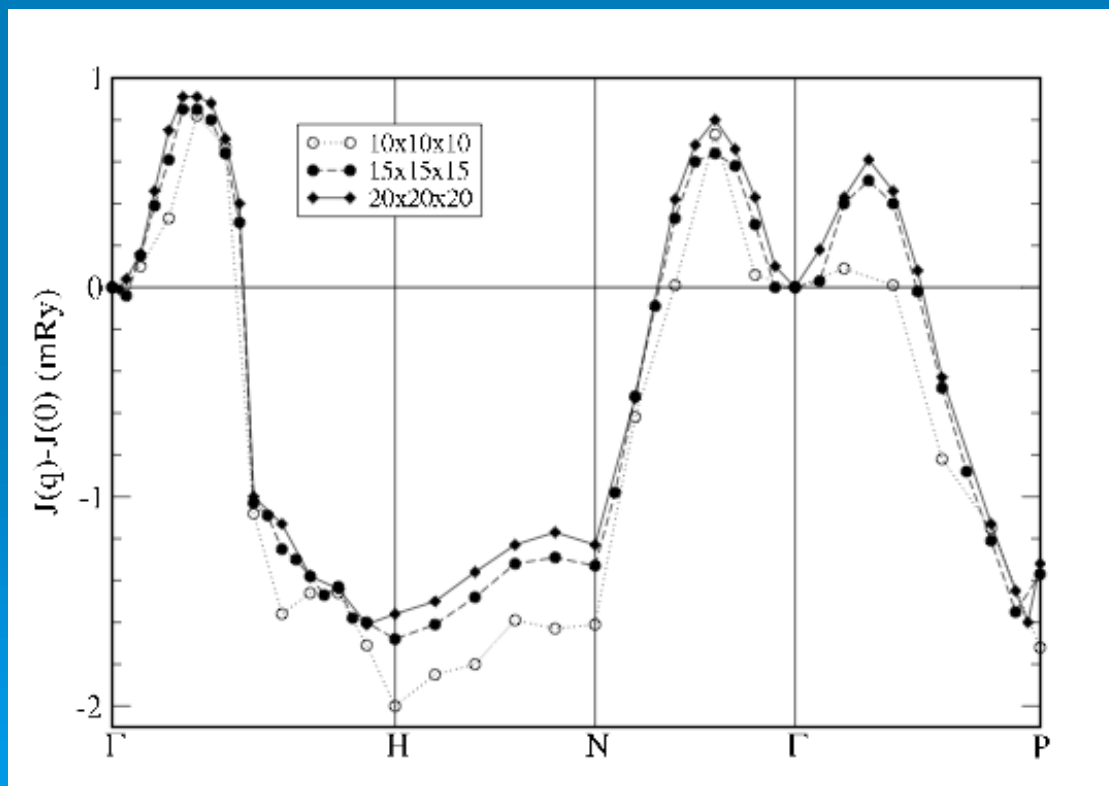
# Band structure



# Spin spirals - $J(\mathbf{q})$

$$H = \frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

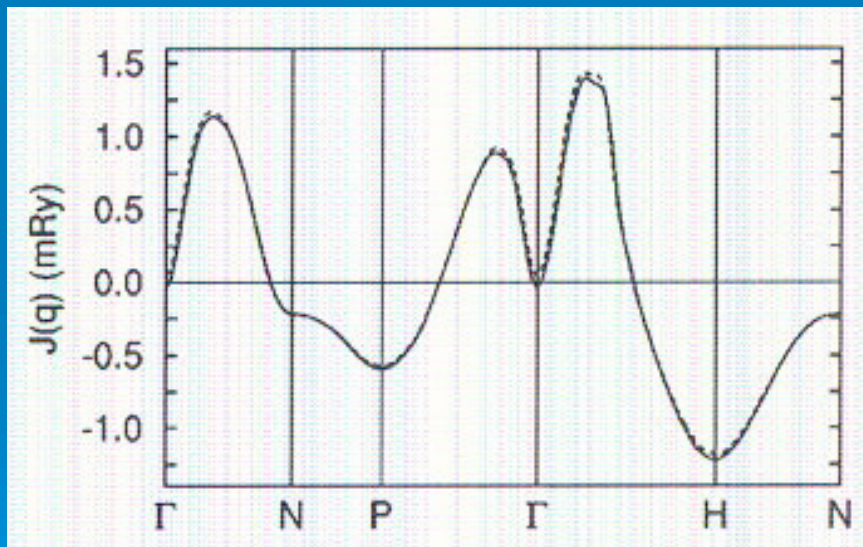
$$J(\mathbf{q}) = \sum_i e^{i\mathbf{q} \cdot \mathbf{R}_i} J_{0i}$$



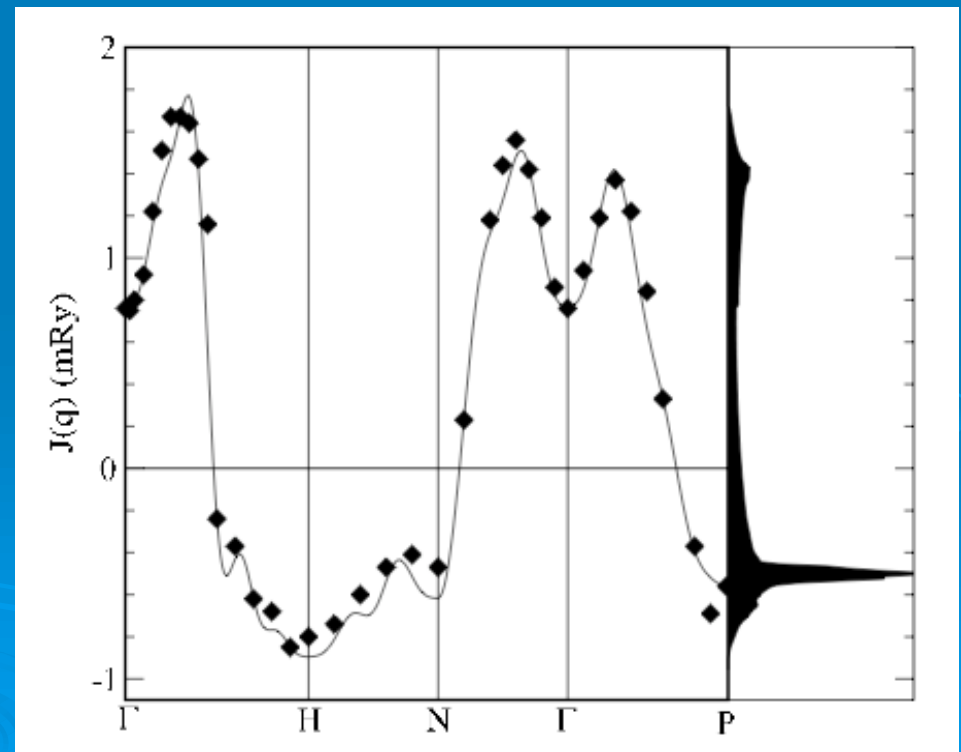
# Normalized $J(\mathbf{q})$

Goldstone sum rule:

$$\int_{BZ} d\mathbf{q} J(\mathbf{q}) = 0$$

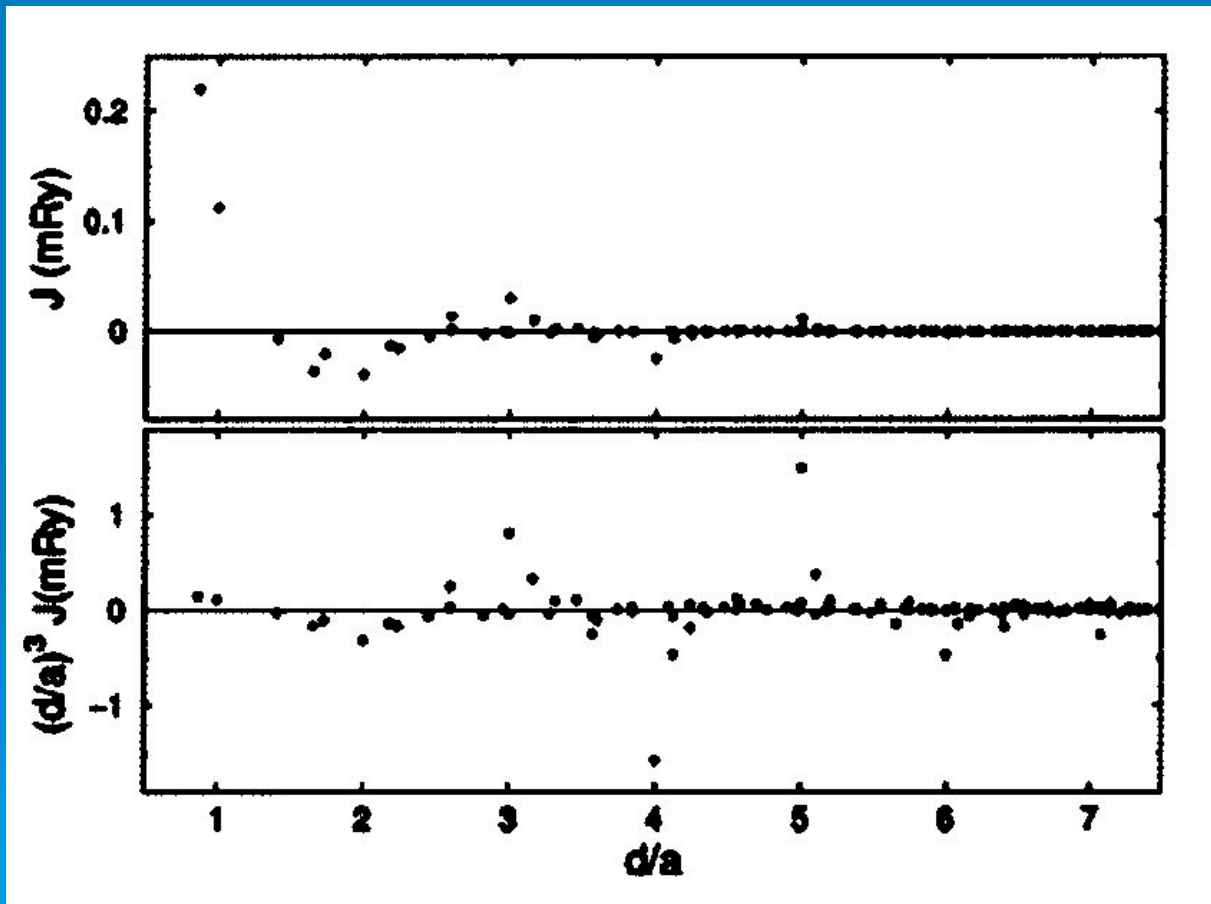


Turek *et al.* PRB **68** 224431 (2003)  
real space LMTO calculation



# Real space exchange parameter $J_{0R}$

Long range  $J_{ij}$  ; RKKY oscillations:



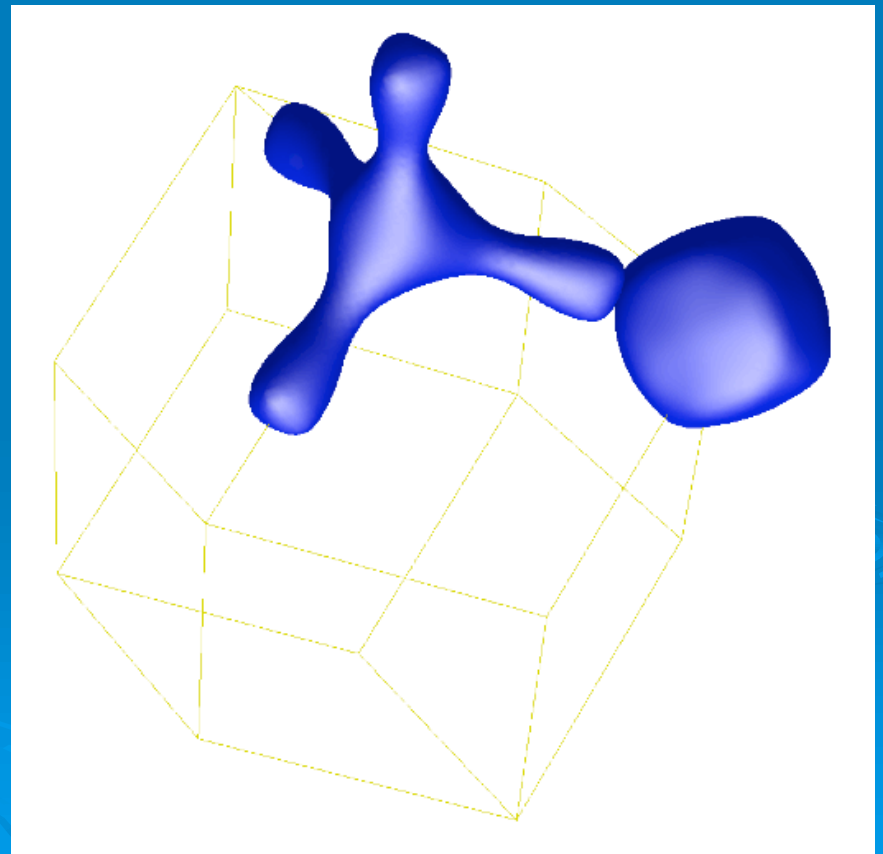
# Fermi surface

Generalized susceptibility

$$\chi(\omega, \mathbf{q}) = \sum_{\mathbf{k}} \frac{f(\epsilon_{\mathbf{k}+\mathbf{q}}) - f(\epsilon_{\mathbf{k}})}{\omega + \epsilon_{\mathbf{k}+\mathbf{q}} - \epsilon_{\mathbf{k}}}$$

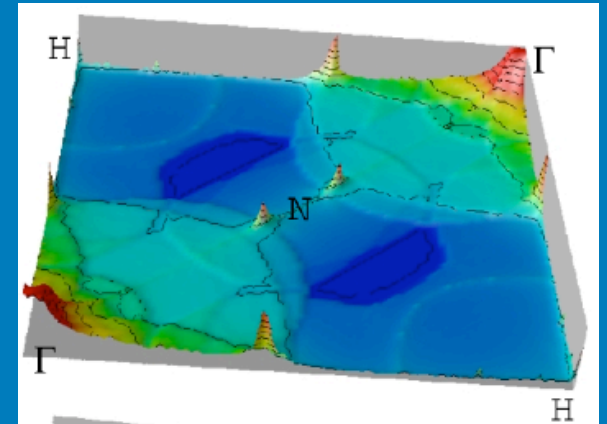
Two sheets of FS:

Lobed tetrahedron - P  
Rounded cube - H

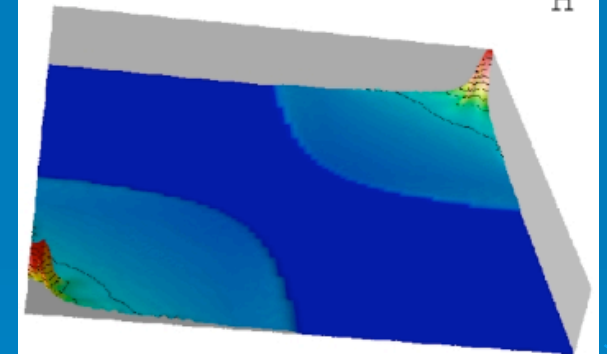


# Generalized susceptibility

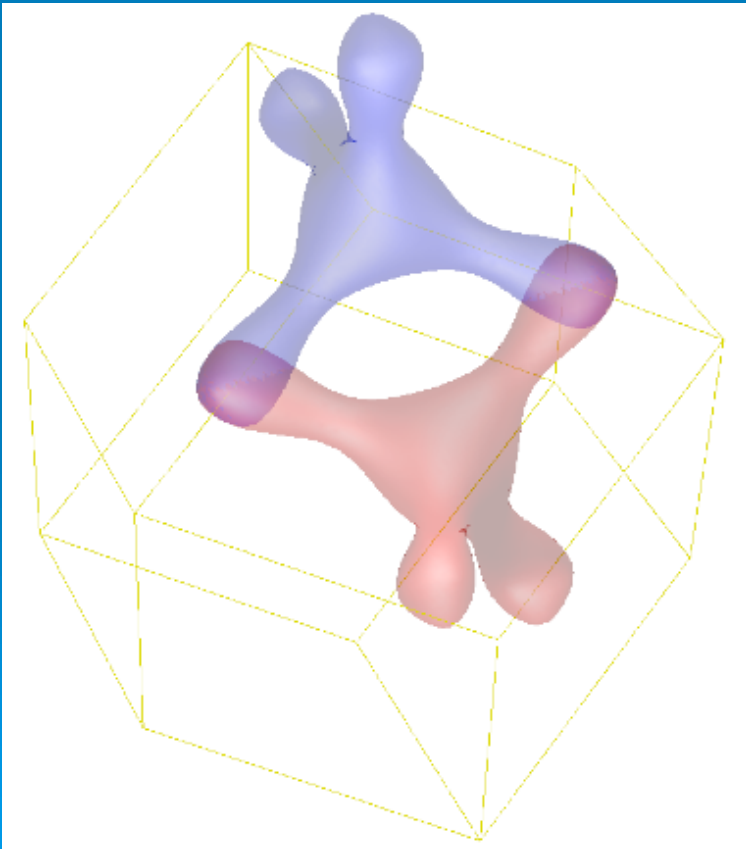
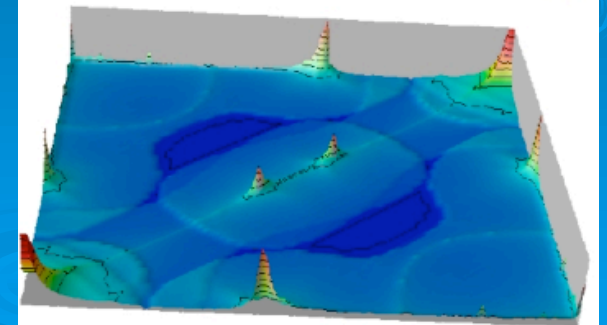
Total:



Rounded  
cube:



Lobed  
tetrahedron:



# bcc Eu - summary

- Ordering temperature  $T=112$  K (exp. 91 K)
- Spiral propagation vector  $q \parallel$  cubic axis associated with a nesting feature of the paramagnetic FS
- $J_{f \cdot s_d}$  coupling of local moments
- RKKY type of inter-site coupling

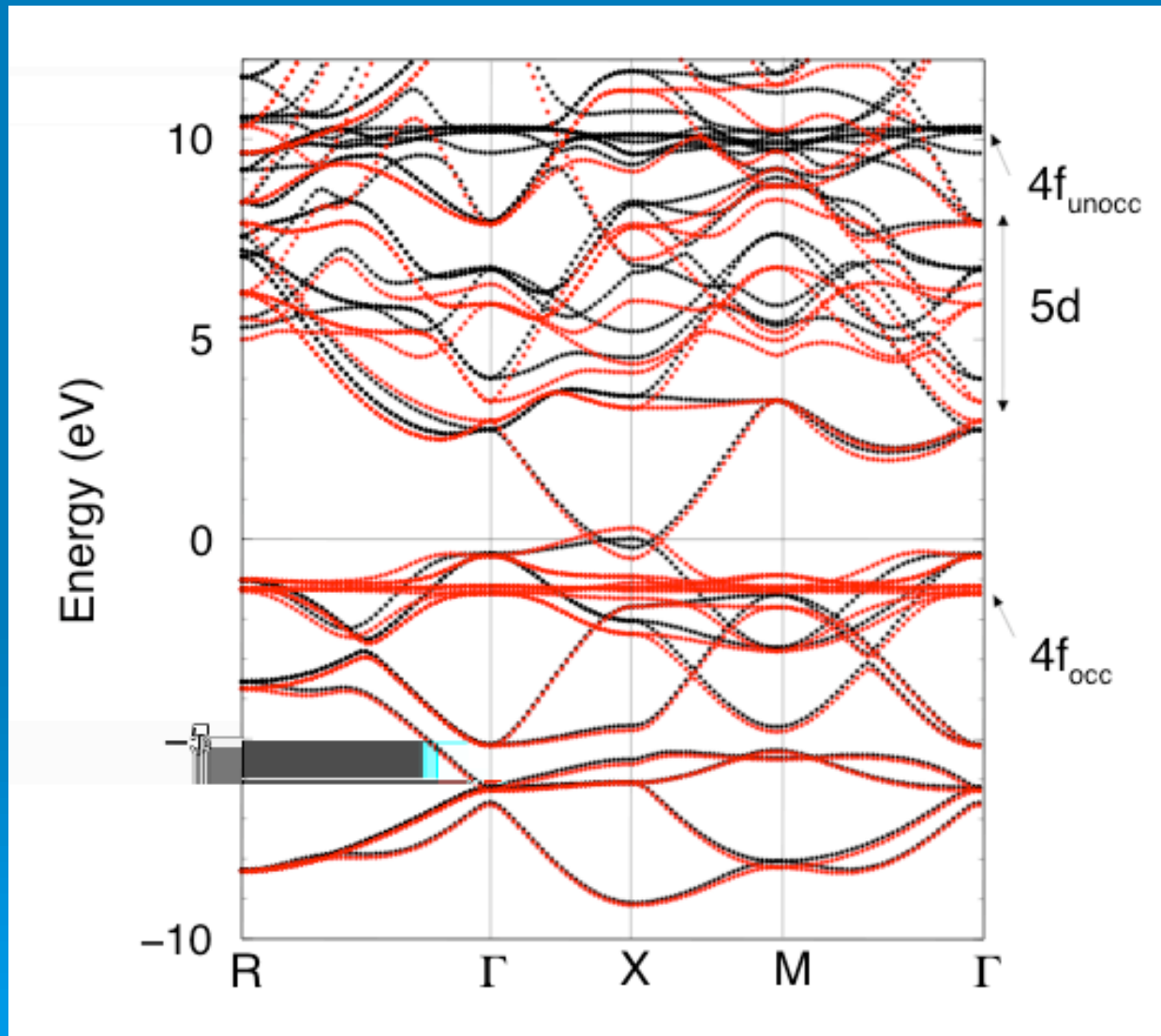


# EuB<sub>6</sub>

- Simple cubic structure
- Eu<sup>2+</sup> valency
- Ground state unclear (semimetal vs narrow gap insulator)
- Two magnetic transitions (15.1K & 12.7 K)
- Colossal magneto-resistance

Nature of ground state? Magnetic properties?

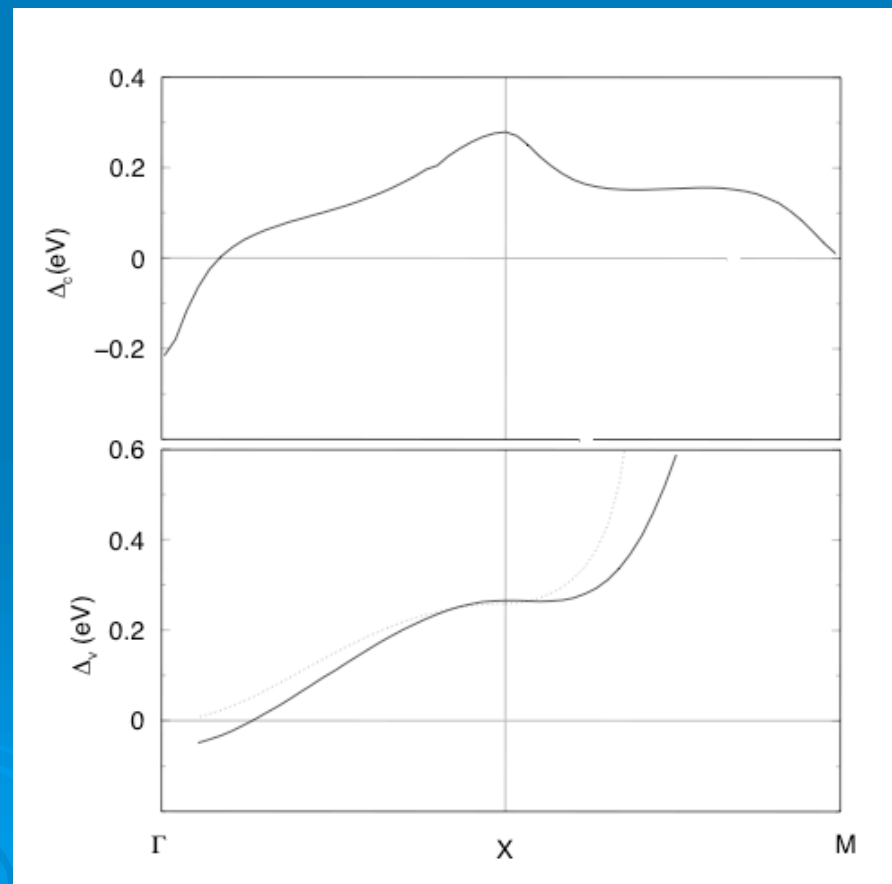
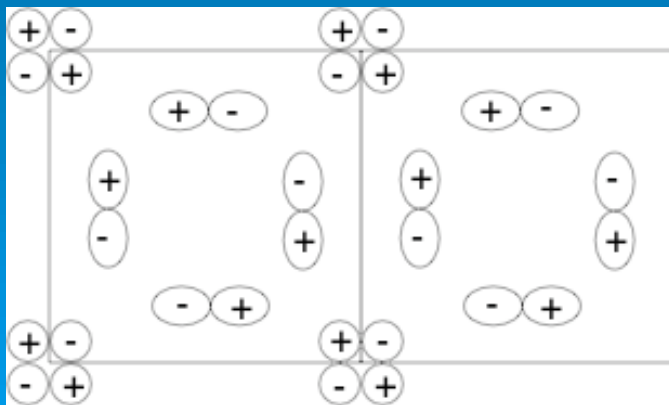
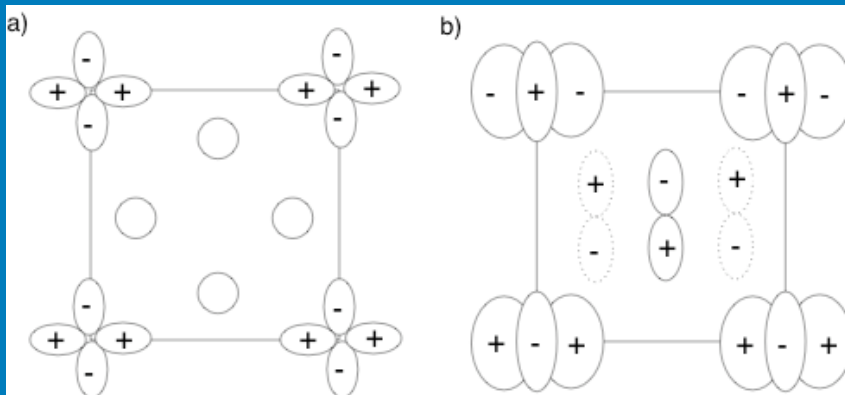
# Spin polarized band structure



# Exchange splitting

Orbitals at X point:

Splitting between spin up and down bands:



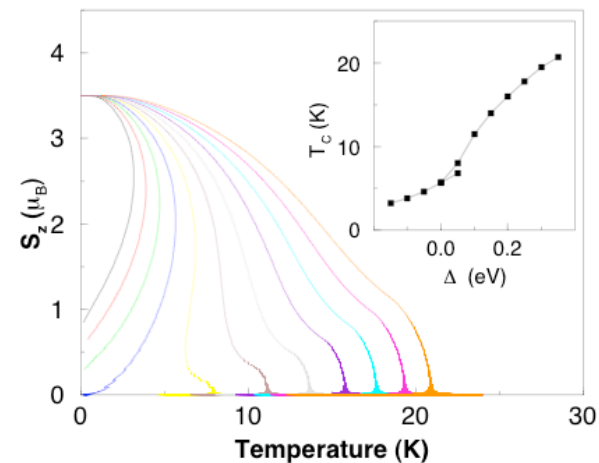
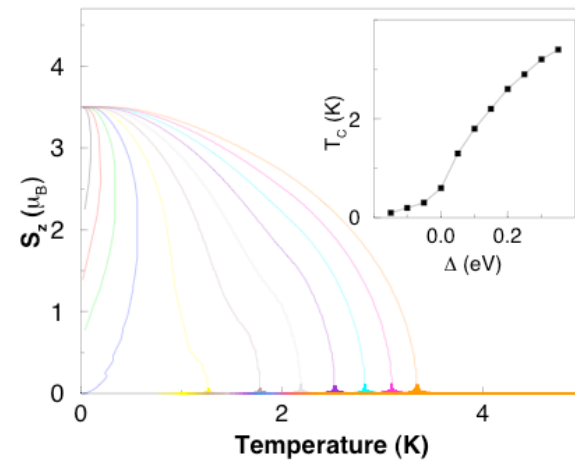
# Molecular field model

Magnetization curves as a function of band gap (overlap) and exchange parameter J:

$$H_{MF} = \sum_{\mathbf{k}, \sigma} [\epsilon_{\mathbf{k}\sigma}^v v_{\mathbf{k}\sigma}^\dagger v_{\mathbf{k}\sigma} + \epsilon_{\mathbf{k}\sigma}^c c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}\sigma}] - \sum_i h S_i^z$$

$$h = \sum_{\sigma} \sigma (J^c n_c^{\sigma}(S^z) - J^v n_v^{\sigma}(S^z))$$

$$S^z = B_{7/2} \left( \frac{h}{k_B T} \right),$$



# EuB<sub>6</sub> - summary

- The local moments are FM coupled to the conduction band and AFM coupled to the valence band
- AFM coupling can be understood in terms of band mixing (Schrieffer-Wolff transformation), FM coupling is due to intra-atomic f-d exchange
- This type of exchange leads to magnetization dependent carrier concentration