

The delicate electronic and magnetic structure of the LaFePnO system (Pn = pnictogen)

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New Journal of Physics **11** (2009) 025004 (26pp)

Received 25 September 2008

Published 27 February 2009

Online at <http://www.njp.org/>

doi:10.1088/1367-2630/11/2/025004

Abstract. The occurrence of high-temperature superconductivity, and the competition with magnetism, in stoichiometric and doped LaFeAsO and isostructural iron oxypnictides is raising many fundamental questions about the electronic structure and magnetic interactions in this class of materials. There are now sufficient experimental data that it may be possible to identify the important issues whose resolution will lead to the understanding of this system. In this paper, we address a number of the important issues. One important characteristic is the Fe–As distance (or more abstractly the pnictogen (Pn) height $z(\text{Pn})$); we present results for the effect of $z(\text{Pn})$ on the electronic structure, energetics and Fe magnetic moment. We also study LaFeAsO under pressure, and investigate the effects of both electron and hole doping within the virtual crystal approximation. The electric field gradients for all atoms in the LaFeAsO compound are presented (undoped and doped) and compared with available data. The observed (π, π, π) magnetic order is studied and compared with the computationally simpler $(\pi, \pi, 0)$ order which is probably a very good model in most respects. We investigate the crucial role of the pnictogen atom in this class, and predict the structures and properties of the N and Sb counterparts that have not yet been reported experimentally. At a certain volume a gap opens at the Fermi level in LaFeNO, separating bonding from antibonding bands. This is the first evidence that this class of materials indeed has an

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underlying semimetallic character, and this separation suggests directions for a better simple understanding of the seemingly intricate electronic structure of this system. Finally, we address briefly differences resulting from substitution of post-lanthanum rare earth atoms, which have been observed to enhance the superconducting critical temperature substantially.

Contents

1. Background and motivation	2
2. Crystal structure	3
3. Calculation method	4
4. Study of LaFeAsO in the tetragonal structure	5
4.1. Influence of XC functionals and codes on the electronic structure of LaFeAsO	5
4.2. Effect of $z(\text{As})$ on the electronic structure of LaFeAsO	6
4.3. Effect of virtual crystal doping on the electronic structure of LaFeAsO	7
4.4. Electric field gradients (EFG)	8
4.5. Effect of pressure on the electronic structure of LaFeAsO	9
5. Investigation of the structural distortion and of the (π, π, π) magnetic order	11
5.1. $(\pi, \pi, 0)$ structural order	11
5.2. (π, π, π) magnetic order	16
6. Role of the pnictogen atom	17
6.1. LaFePO	18
6.2. LaFeSbO	20
6.3. LaFeNO	21
7. Role of the rare earth atom in ReFeOAs	22
8. Summary	24
Acknowledgments	25
References	25

1. Background and motivation

The layered conductors LaFePO and LaFeAsO, though isostructural and isovalent, display surprisingly different properties. The first is nonmagnetic and was initially reported as superconducting with critical temperature $T_c = 2\text{--}7\text{ K}$ [1]–[4], while more recently there are indications [5, 6] that stoichiometric LaFePO may not be superconducting without the presence of oxygen vacancies. The second compound becomes antiferromagnetically ordered at $T_N \approx 140\text{ K}$ [7, 8] with no report of superconductivity in the stoichiometric compound. The discovery of superconductivity at 26 K in carrier-doped LaFeAsO [9], followed by rapid improvement now up to $T_c = 55\text{ K}$ [13] in this class, is strikingly different from what is reported in LaFePO and these high values of T_c make these superconductors second only to the cuprates in critical temperature. Several dozen preprints appeared within the 2 months after the original publication, and many hundreds since, making this the most active field of new materials study in recent years (since the discovery of superconductivity in MgB_2 , at least).

A host of models and ideas about the ‘new physics’ that must be operating in this class of compounds is appearing, pointing out the need to establish a clear underpinning of the basic

electronic (and magnetic) structure of the system. The materials are strongly layered, quasi-two-dimensional in their electronic structure, by consensus [1, 9]. The electronic structure of LaFePO was described by Lebègue [14], with the electronic structure and its neighboring magnetic instabilities of LaFeAsO being provided by Singh and Du [15]. Several illuminating papers have appeared since, outlining various aspects of the electronic and magnetic structure of LaFeAsO.

The extant electronic structure work has provided a great deal of necessary information, but still leaves many questions unanswered, and indeed some important questions are unaddressed so far. One very relevant result is the resonant x-ray emission at the Fe L-edge and non-resonant O and F K-edge data of Kurmaev *et al* [16]. Since they observe no indication of the lower Hubbard band or a quasiparticle peak that would accompany strong intra-atomic interactions on the Fe atom, conventional density functional methods seem to be the method of choice for establishing the underlying picture of the electronic and magnetic behavior of these materials. In this paper, we address some of these questions more specifically. Stoichiometric LaFeAsO is AFM; then ~ 0.05 carriers/Fe doping of either sign destroys magnetic order and impressive superconductivity arises, with T_c seemingly depending little on the carrier concentration [9, 17] (reports on other families, such as $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ [10], indicate that T_c can be strongly dependent on the amount of doping). BaFe_2As_2 and SrFe_2As_2 , on the other hand, transform directly from nonsuperconducting antiferromagnet to high-temperature superconductors under pressure, without any doping whatever [11, 12].

The question we address here can be typified by the question: with the nonmagnetic electronic structure of LaFePO and LaFeAsO being so similar, why are their magnetic and superconducting behavior so different? Surely this difference must be understood and built into bare-bones models, or else such models risk explaining nothing, or explaining anything. Another question is the effect of the structure. Unusual sensitivity to the As height $z(\text{As})$ has been noted [18]; T_c is reported to increase with applied pressure [19, 20] (reduction in volume) for low values of doping (up to $x = 0.11$ in $\text{LaFeAsO}_{1-x}\text{F}_x$, which is reported as the amount of F for optimal doping); there are increases in T_c due to replacement of La with other rare earth ions, and the variation in size of the rare earth is often a dominant factor in the observed trends in their compounds. Very important also is the magnetism in these materials, since magnetism is a central feature in the cuprate superconductors and in correlated electron superconductors. Another important question is: what can be expected if other pnictide atoms can be incorporated into this system: Sb (or even Bi) on the large atom side, or N on the small atom end. In this paper, we address these questions.

2. Crystal structure

The members of the family of the new Fe-based superconductors crystallize in the ZrCuSiAs type structure [21, 22] (space group $P4/nmm$, $Z = 2$). For instance, LaFeAsO is made of alternating LaO and FeAs layers, as presented in figure 1. The Fe and O atoms lie in planes, whereas the As and La atoms are distributed on each side of these planes following a chessboard pattern. The crystal structure is fully described by the a and c lattice parameters, together with the internal coordinates of La and As. Experimentally, $a = 4.03533 \text{ \AA}$ and $c = 8.74090 \text{ \AA}$, whereas $z(\text{La}) = 0.14154$ and $z(\text{As}) = 0.6512$. However to describe correctly the antiferromagnetic (AFM) structure, a $\sqrt{2}a \times \sqrt{2}a \times c$ cell must be used, with four Fe atoms per cell, as shown in full lines in figure 2. We will refer to this AFM order as the Q_M AFM order,

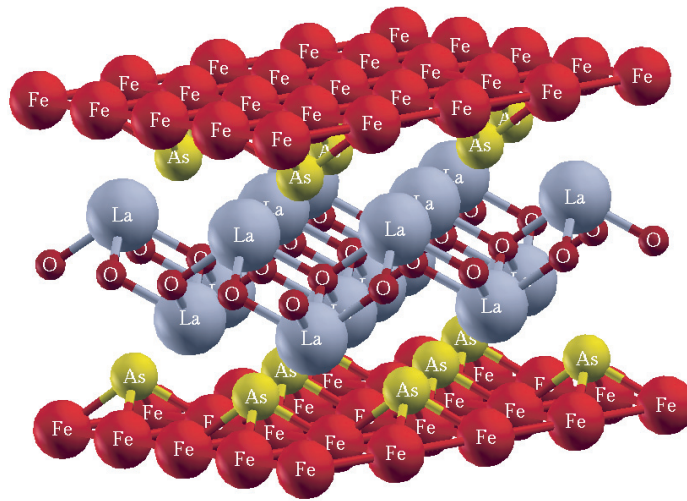


Figure 1. The crystal structure of LaFeAsO, showing the alternating layers of LaO and FeAs.

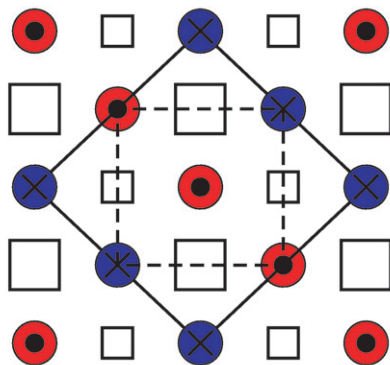


Figure 2. The Q_M magnetic structure of the Fe–As substructure of LaFeAsO, showing alternating chains of Fe spin up (red circles with black dots) and Fe spin down (blue circles with black crosses). The As atoms above (below) the Fe plane are represented as large (small) squares. The $\sqrt{2}a \times \sqrt{2}a \times c$ cell is represented with full lines, whereas the $a \times a \times c$ cell is with dashed lines.

or equivalently as $(\pi, \pi, 0)$, whereas the Q_0 AFM order corresponds to an AFM order of the original cell (dashed lines in figure 2) with two Fe atoms. Also, FM will refer to a ferromagnetic arrangement of the spins, whereas NM means non-magnetic.

3. Calculation method

To calculate the relevant quantities, we have used density functional theory (DFT) [23, 24], as implemented in three different electronic structure codes. The full potential local orbital (FPLO) code [25, 26] was mainly used, while we double checked some of the calculations with WIEN2k code [27]. For most of the FPLO and LAPW calculations, the Perdew and Wang 1992 (PW92) [28] exchange-correlation (XC) functional was used, but the effect of XC

functional was checked using also local spin density approximation (LSDA)(PZ) [29], the PBE functional [30] and another generalized gradient approximation (GGA) [31] XC functional. At each chosen volume, the crystal structure was fully relaxed, i.e. c/a , $z(\text{La})$ and $z(\text{Pn})$ were relaxed, where Pn is the pnictogen atom. The uncertainties were estimated to be within 0.5% for c/a and 0.0002 for $z(\text{La})$ and $z(\text{Pn})$. The relaxation was performed in the Q_M AFM structure, with 132 irreducible k points in the Brillouin zone (BZ). We double checked the total energy with a finer mesh with 320 irreducible k points in the BZ and the difference was very small. After relaxation, all calculations were performed using dense meshes, with 320, 1027 and 637 irreducible k points in the BZ of the Q_M AFM, Q_0 AFM and NM structures, respectively. In the Q_M AFM structure, we used 464 irreducible k points in the BZ to double check the result, without any noticeable difference in the density of states (DOS) nor band structure. As for the results presented in section 5, we used the projector augmented waves (PAW) method [32] as implemented in the code Vienna *Ab-initio* Simulation Package (VASP) [33, 34]. The PBE [30] variant of the GGA was used for the XC potential. A cut-off of 600 eV was used for the plane-wave expansion of the wave function to converge the relevant quantities. For BZ integrations, a mesh of $9 \times 9 \times 7$ k -points [35] was used as an input to the modified tetrahedron method [36]. This mesh was decreased to $9 \times 9 \times 3$ for the cell doubled along the c -axis.

4. Study of LaFeAsO in the tetragonal structure

LaFeAsO has a tetragonal structure (as described in section 2) at room temperature [9]. Although it undergoes a structural phase transition at lower temperature [7, 8] (see section 5), the doped (and superconducting) material $\text{LaO}_{1-x}\text{F}_x\text{FeAs}$ remains in this structure down to low temperature [7, 8], so the study of LaFeAsO in the high-symmetry structure is a necessary step towards the understanding of the electronic structure of the whole family of compounds.

4.1. Influence of XC functionals and codes on the electronic structure of LaFeAsO

Initially, we studied the electronic structure of LaFeAsO in the experimental (tetragonal) crystal structure for different magnetic states (Q_M AFM, Q_0 AFM, FM and NM) using two different codes (FPLO7 and WIEN2k) and different XC functionals. This is necessary in view of the large number of theoretical papers [15], [37]–[49] which appeared recently and often disagree on certain results. This was partly studied by Mazin *et al* [50]. Table 1 summarizes the results: the magnetic moment on the Fe atom together with the total energy differences for each magnetic state studied here. Independently of the code or the XC functionals used, the Q_M AFM state is always found to be the ground state, which confirms our earlier report [18]. The magnetic moments for both types of AFM order are considerably larger than the ordered moment reported from neutron diffraction [7] and muon spin relaxation experiments, [17, 65], whereas the one for the FM order is much smaller. For this last case, FPLO7 gives zero (no magnetism) with both PZ and PW92 XC functionals; WIEN2k gives about $0.36 \mu_B$ with GGA and PBE and $0.13 \mu_B$ with PW92. It appears, therefore, that the magnetic moment of Fe for the same state with different XC functionals and codes varies by up to $0.5 \mu_B$. Although GGA is known to enhance the tendency toward magnetism [50] compared with local density approximation (LDA), these sensitivities are unusually large and comprise an additional peculiar aspect of this class of materials. The difference between FPLO7 and WIEN2k in predicting the Fe magnetic moment for each state may explain the total energy differences among them. Virtual doping (see section 4.2)

Table 1. Calculated magnetic moment of Fe, the amounts of total energy per Fe lie below nonmagnetic state of FM, Q_0 AFM and Q_M AFM states from FPLO7 and WIEN2k with different XC functionals of LaFeAsO with experimental structure. Positive ΔEE means lower total energy than NM state.

Code	XC	Magnetic moment (μ_B)			ΔEE (meV Fe $^{-1}$)		
		Q_M	Q_0	FM	Q_M	Q_0	FM
FPLO7	PW92	1.87	1.72	0.00	87.2	24.6	0
	PZ	1.70	1.31	0.00	62.2	6.9	0
WIEN2k	PW92	1.74	1.52	0.13	136.9	78.9	0
	GGA	2.09	1.87	0.36	149.1	65.2	3.7
	PBE	2.12	1.91	0.37	158.1	70.2	4.5
0.1e $^{-}$ doped	PW92	1.86	–	0.08	125.2	–	–0.5
0.1e $^{-}$ doped	GGA	2.14	–	0.26	139.7	–	–0.1
0.1e $^{-}$ doped	PBE	2.16	–	0.27	149.6	–	2.1

by 0.1 e $^{-}$ /Fe enhances the Fe magnetic moment in the Q_M AFM state but reduces it in the FM state for all the XC functionals used.

In the structural optimization (performed in the Q_M state), FPLO7 with PW92 (LDA) functional gives reasonable c/a and $z(\text{La})$ in good agreement with experiment, but it predicts $z(\text{As}) \sim 0.639$, which is 0.011 off the experimental value, about 0.1 Å discrepancy in the Fe–As separation. However, WIEN2k with the PBE(GGA) XC functional gives an optimized $z(\text{As}) \sim 0.649$, which agrees well with experimental $z(\text{As})$. Similar results are found in the XFe_2As_2 family (X = Ba, Sr, Ca). This suggests that the GGA (PBE) XC functional optimizes the FeAs-based system much better than LDA (PW92) XC functional. If so, then GGA should have better performance in dealing with the structure (including c/a , equilibrium volume and $z(\text{As})$) under pressure of this FeAs family. This is probably due to the layered structure of the FeAs family which results in large density gradient between layers, thus GGA gives a better description of the potential. On the downside, GGA (PBE) further overestimates the magnetic moment of Fe, which is already overestimated by LDA (PW92).

4.2. Effect of $z(\text{As})$ on the electronic structure of LaFeAsO

Next, we studied how the electronic structure of LaFeAsO depends on the value of $z(\text{As})$. Table 2 shows the difference between the experimental $z(\text{As})$ (~ 0.650), the optimized $z(\text{As})$ (~ 0.639) and a middle value of 0.645 when using FPLO7 with the PW92 XC functional. Decreasing $z(\text{As})$ (reducing the Fe–As distance) rapidly reduces the differences in energy between the different magnetic orderings. At $z(\text{As}) = 0.645$, the magnetic moments of the Q_M and Q_0 states are reduced significantly in comparison with $z(\text{As}) = 0.650$, and the difference in energy has changed by around 20%, indicating important changes in the electronic structure upon moving the As atom. For $z(\text{As}) = 0.639$, the Q_0 AFM state has lost its moment (become the NM state), whereas the magnetic moment of the Q_M state has decreased even more, with a changing rate of 6.8 $\mu_B \text{ \AA}^{-1}$, indicating strong magnetophonon coupling [18]. Therefore, using the experimental or optimized value for the internal coordinate of As gives quite different results and might explain several of the discrepancies seen in the previously published works. In

Table 2. Calculated magnetic moment of Fe, total energy relative to the nonmagnetic (ferromagnetic) states of NM/FM, Q_0 AFM and Q_M AFM of LaFeAsO with $z(\text{As}) = 0.650$ (experimental), 0.645 and 0.639 (optimized) from FPLO7 with PW92 XC functional.

$z(\text{As})$	Magnetic moment (μ_B)			$\Delta E E$ (meV Fe $^{-1}$)		Fe 3d occ.#	
	Q_M	Q_0	FM	FM- Q_M	Q_0 - Q_M	maj.	min.
0.650	1.87	1.72	0.002	87.2	62.6	4.32	2.45
0.645	1.70	1.41	0.000	60.5	54.0	4.24	2.55
0.639	1.48	0.01	0.000	34.6	34.6	4.15	2.68

figures 3 and 4, we present the corresponding band structures, total densities of states and partial densities of states calculated for different values of $z(\text{As})$. Surprisingly, the band structure near E_F referred to the common Fermi level barely changes when $z(\text{As})$ decreases. Somewhat away from E_F , the bands below the Fermi level are pushed up in energy when $z(\text{As})$ is decreased, while the effect of the Fe–As distance on the bands above E_F is less obvious, since they are pushed up or down depending on the direction of the BZ. For instance, along Γ – X and Γ – Z they are pushed down, so that a decrease of the pseudogap is expected, as shown by figure 3. The peaks of the DOS just above Fermi level move toward it when $z(\text{As})$ is reduced, whereas the DOS below the Fermi level is more robust. The important decrease of the magnetic moment of Fe when the Fe–As distance changes is understood by looking at the Fe 3d partial density of states (PDOS) (figure 4) and the last column of table 2. Although the number of Fe 3d electrons remains approximately constant, the number of spin up electron decreases, whereas the number of spin down electrons is increased when $z(\text{As})$ is reduced, accounting for the decrease of the magnetic moment.

4.3. Effect of virtual crystal doping on the electronic structure of LaFeAsO

Since superconductivity arises in LaFeAsO only when it is doped, it becomes important to know how doping will affect the underlying electronic structure and the character of each magnetic state. Using the experimental lattice parameters, we performed virtual crystal doping calculations on LaFeAsO using WIEN2k by changing the charge of O (doping with F) and La (doping with Ba, but simulating doping with Sr as well), and the corresponding number of valence electrons. The virtual crystal method is superior to a rigid band treatment because the change in carrier density within the Fe–As subsystem is calculated self-consistently in the average potential of the alloy.

There is only a weak dependence of the calculated Fe magnetic moment on the electron doping level: 0.1 e $^-$ /Fe doping enhances it from 2.12 to 2.16 μ_B (see table 1). However, electron doping reduces the total energy difference (compared to NM) in both Q_M AFM and FM states. The main effect of virtual crystal doping is to change the Fermi level position, in roughly a rigid band fashion (see the caption of figure 5 for more details). The band structures of 0.1 and 0.2 e $^-$ /Fe doped LaFeAsO in the Q_M AFM phase show only small differences; the charge goes into states that are heavily Fe character and the small change in the Fe 3d site energy with respect to that of As 4p states is minor.

Notably, the virtual crystal approximation continues to give strong magnetic states, whereas doping is observed to degrade and finally kill magnetism and promote superconductivity. Thus

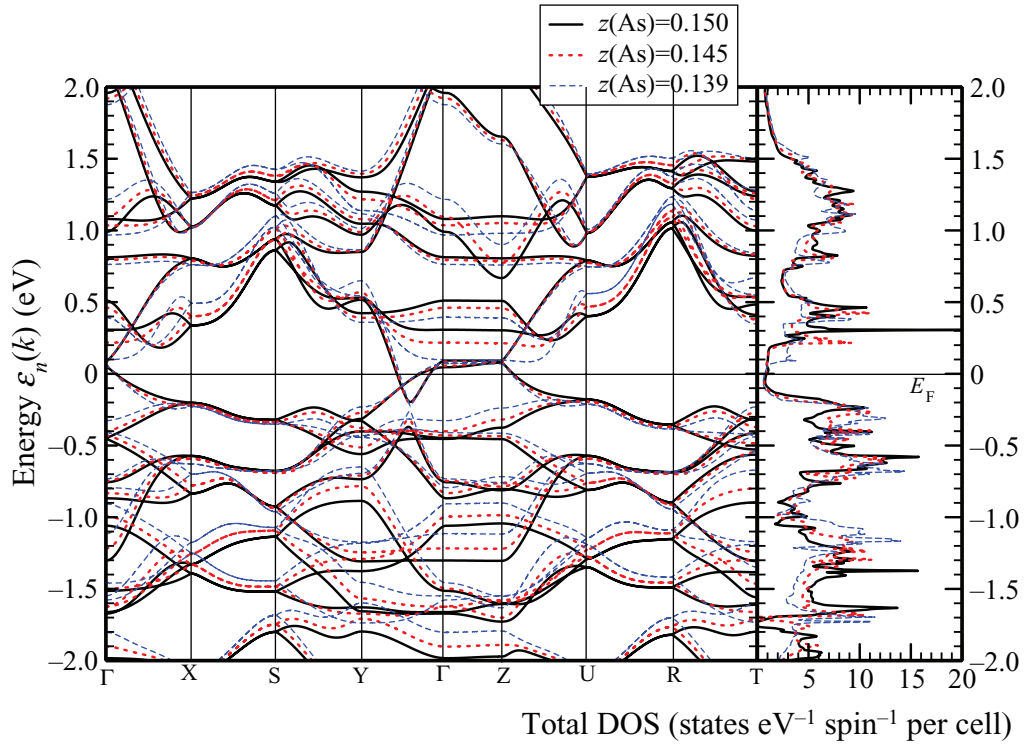


Figure 3. The bandstructure and total DOS of Q_M LaFeAsO at ambient pressure computed for $z(\text{As}) = 0.650$, $z(\text{As}) = 0.645$ and $z(\text{As}) = 0.639$.

the destruction of magnetism requires some additional effect not considered here, such as strong dynamical spin fluctuations that are sensitive to doping level.

4.4. Electric field gradients (EFG)

We have calculated the EFG of each atom in LaFeAsO, studying both the effects of doping and of magnetic order. The structure used for these calculations is $a = 4.0355 \text{ \AA}$, $c = 8.7393 \text{ \AA}$, $z(\text{La}) = 0.142$, $z(\text{As}) = 0.650$ and the PBE(GGA) XC functional was used in the WIEN2k code. (The PW92 (LDA) XC functional gives similar results and thus the results are not presented here.) Since the EFG is a traceless symmetric 3×3 matrix, only two of V_{xx} , V_{yy} , V_{zz} are independent. For cubic site symmetry, the EFG vanishes, hence the magnitude and sign of the EFG reflects the amount and character of anisotropy of the charge density. For the symmetries studied here, the off-diagonal components of the EFG tensor for all four atoms are zero. For the Q_M AFM state, the V_{yz} component calculated separately for each spin for La and As is not zero, although the sum vanishes; the spin decomposition gives information about the anisotropy of the spin density that is not available from measurements of the EFG.

As shown in tables 3 and 4, the EFGs of both Fe and As in NM and FM states are very similar and they are doping insensitive, except for Fe where the EFG is comparatively small. Due to the breaking of the x - y symmetry in the Q_M phase, V_{xx} is no longer equal to V_{yy} . In this case, the EFGs are quite different from those in the NM and FM states, which shows once more that the electronic structure in the Q_M AFM order differs strongly from the ones of the NM and FM orders. Also, while hole doping (on the La site) and electron doping (on

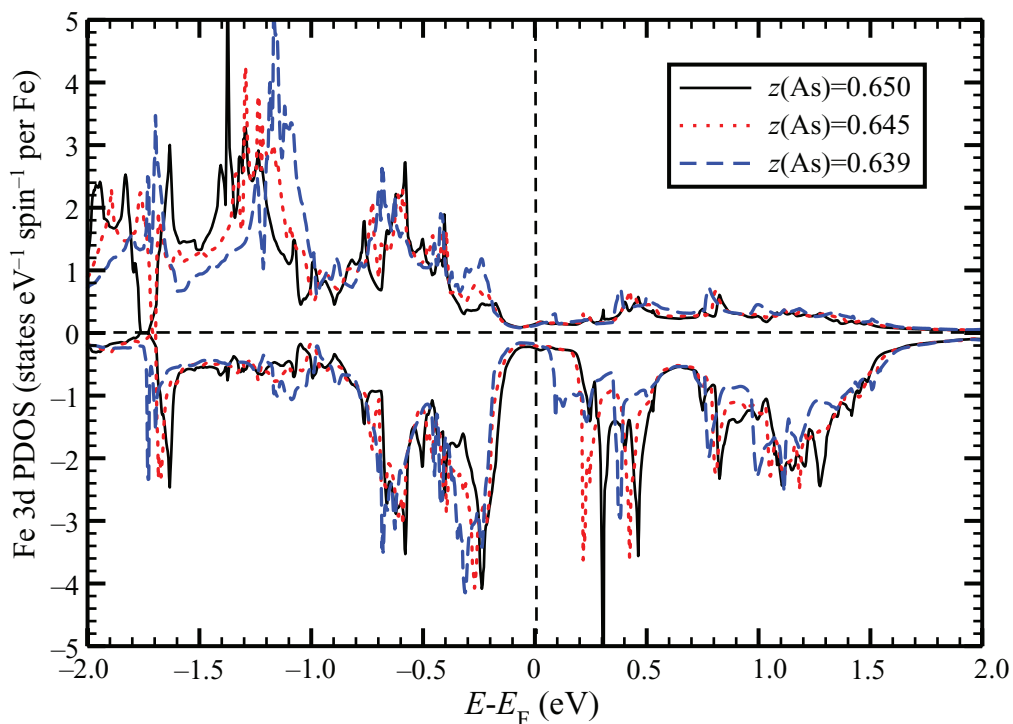


Figure 4. Plot of LaFeAsO Q_M AFM Fe 3d PDOS at ambient pressure with $z(\text{As}) = 0.650$, $z(\text{As}) = 0.645$ and $z(\text{As}) = 0.639$.

the O site) significantly change the EFG of Fe, the EFG of As is less affected. Using nuclear quadrupolar resonance (NQR) measurement, Grafe *et al* [51] reported a quadrupole frequency $\nu_Q = 10.9$ MHz and an asymmetry parameter $\eta = 0.1$ of the As EFG in LaFeAsO_{0.9}F_{0.1}. This observation gives $V_{zz} \sim 3.00 \times 10^{21}$ V m⁻², which agrees reasonably well with our result of 2.6×10^{21} V m⁻² as shown in table 4 in the NM state. Upon 0.1 electron or 0.1 hole doping, the EFGs for As are barely changed but some of them are changed substantially for Fe.

4.5. Effect of pressure on the electronic structure of LaFeAsO

Applying pressure is often used as a way to probe how the resulting effect on the electronic structure impacts the superconducting critical temperature and other properties. A strong pressure effect was shown experimentally for the members of the LaFeAsO family [19, 20, 52], since for example $T_c = 43$ K could be reached under pressure for LaO_{1-x}F_xFeAs, in the case of optimal doping [19]. To begin to understand such observations, it is necessary to determine how the electronic structure of the parent compound LaFeAsO is changed by pressure.

In figure 6, the magnetic moment of Fe in the Q_M AFM phase versus Fe–As distance is presented. Two different types of behavior of the magnetic moment are observed. When $z(\text{As})$ is varied at constant volume (zero pressure), the decrease of the magnetic moment of Fe is parabolic. When pressure is applied and all internal positions are optimized (hence $z(\text{As})$ changes) the change is linear until the magnetic moment drops to zero. This linear behavior is followed also when the As height $z(\text{As})$ is shifted by 0.011 to compensate for the PW92 (LDA) error mentioned above. Figure 7 collects a number of results: the effect of pressure on the c/a

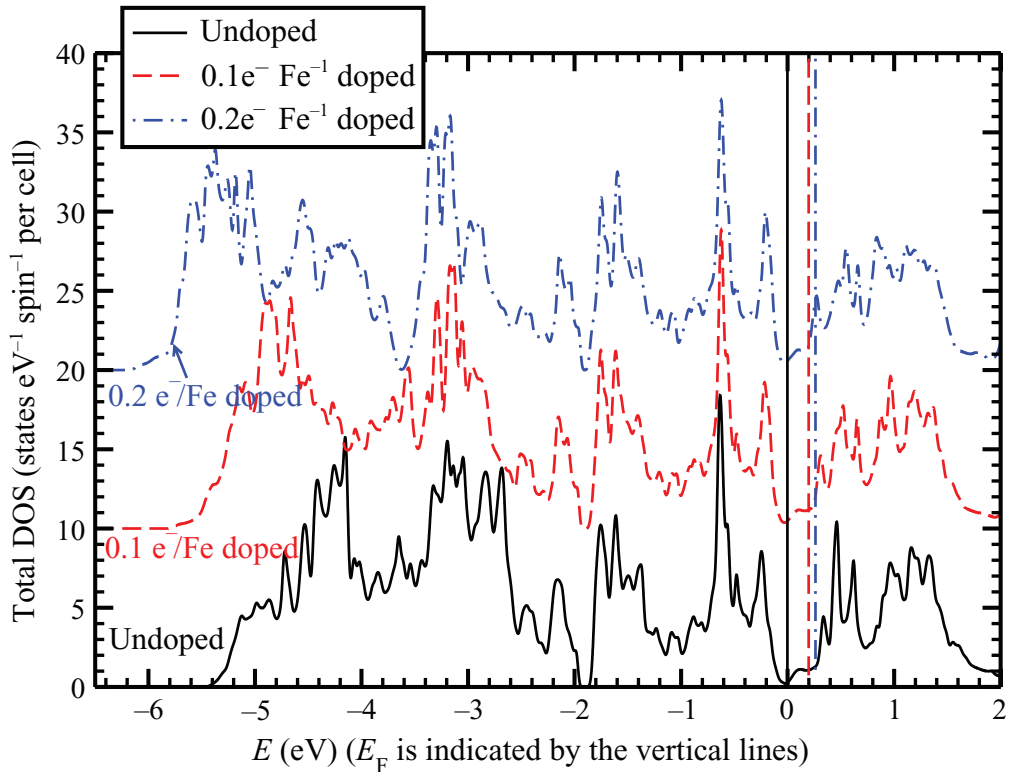


Figure 5. Plots of undoped, 0.1 and 0.2 electron-doped LaFeAsO Q_M AFM total DOS (displaced upward consecutively by ten units for clarity), obtained using the virtual crystal approximation. Referenced to that of the undoped compound, the Fermi levels of 0.1 and 0.2 electron-doped DOS are shifted up by 0.20 and 0.26 eV, respectively.

ratio, the Fe–As distance, the total energy, the difference in energy between NM and QM states and the magnetic moment on Fe. Under pressure, the c/a ratio, the Fe–As distance, and the magnetic moment of the Q_M AFM state drop linearly when volume is reduced. The PW92(LDA) predicts an equilibrium volume of $0.925V_0$; and the total energy differences between NM and Q_M AFM state gradually drop to zero at $0.78V_0$.

The effect of pressure on the band structure is shown in figure 8. While the bands change positions under pressure, in the corresponding DOS (right panel of figure 8), the first peak above E_F is moved towards the Fermi level when pressure is applied, but the DOS from -0.1 eV to E_F is left almost unchanged by pressure. This difference suggests that pressure should induce important changes in the superconducting properties of electron-doped LaFeAsO, while they should be less important for hole-doped LaFeAsO.

The Fermi surface (FS) of Q_M LaFeAsO computed for different values of the volume is presented in figure 9. The first sheet is an almost perfect cylinder along the Γ – Z line, while the second sheet is made of two ellipsoidal cylinders with some k_z bending. They appear to be very similar to the FS computed at ambient pressure [18]. Pressure has almost no effect on the first sheet, but it enhances the distortion of the second sheet.

Table 3. The EFG of Fe in LaFeAsO in the NM, FM and Q_M AFM states at different doping levels, calculated from WIEN2k using the PBE(GGA) XC functional. The unit is 10^{21} V m^{-2} .

Fe doping	V_{xx}			V_{yy}		
	Up	Dn	Total	Up	Dn	Total
NM Undoped	0.11	0.11	0.22	0.11	0.11	0.22
0.1h (La)	0.21	0.21	0.42	0.21	0.21	0.42
0.1e (La)	0.01	0.01	0.02	0.01	0.01	0.02
0.1e (O)	0.09	0.09	0.18	0.09	0.09	0.18
FM Undoped	0.51	-0.30	0.21	0.51	-0.30	0.21
0.1h (La)	0.05	0.39	0.44	0.05	0.39	0.44
0.1e (La)	0.31	-0.21	0.10	0.31	-0.21	0.10
0.1e (O)	0.31	-0.20	0.11	0.31	-0.20	0.11
Q_M Undoped	0.22	0.03	0.25	-1.11	0.54	-0.57
0.1h (La)	0.60	-1.13	-0.43	-1.15	1.04	-0.11
0.1e (La)	-0.55	1.00	0.45	-1.05	0.24	-0.81
0.1e (O)	-0.54	1.01	0.47	-1.07	0.32	-0.75
0.2e (O)	-0.82	1.17	0.35	-1.02	0.52	-0.50

5. Investigation of the structural distortion and of the (π, π, π) magnetic order

Magnetic $\vec{q} = (\pi, \pi, \pi)$ order in stoichiometric LaFeAsO (with the magnetic cell being $\sqrt{2} \times \sqrt{2} \times 2$ relative to the crystallographic cell) was reported first by de la Cruz *et al* [7] using neutron scattering. Ordering takes place at $T_N = 135\text{--}140$ K and is preceded in temperature by a structural distortion occurring around 155 K. These transitions have since been confirmed by other groups [8]. A similar structural distortion was found for NdFeOAs [53], showing that the temperature of the structural phase transition in this case is reduced by about 20 K in comparison with LaFeAsO. These phase transitions have been revisited [54] using various experimental tools (heat capacity, ultrasound spectroscopy, etc.). Although the magnetic ordering of FeAs layers along the c -axis is less likely to be crucial for the mechanism of superconductivity since the involved scale of energy is expected to be very weak in comparison with the intralayer ordering, its study is necessary to understand the complete system. For the same reason, and even if there are strong indications that it does not happen in the case of F-doped LaFeAsO, it is interesting to see whether the structural distortion of pure LaFeAsO can be reproduced by *ab-initio* calculations, and what the change in the electronic structure is. The results we present in this section were obtained using the VASP code with the PBE(GGA) functional [30].

5.1. $(\pi, \pi, 0)$ structural order

The structural transformation [7, 8] changes the $\sqrt{2} \times \sqrt{2}$ cell (with four iron atoms; full lines in figure 2) from tetragonal (space group P4/nmm) to orthorhombic (space group Cmma) or equivalently for the primitive cell (with two iron atoms; dashed lines in figure 2) from tetragonal (space group P4/nmm) to monoclinic (space group P112/n). To simplify our study, the cell doubling along the c -axis due to magnetic ordering is neglected for this study,

Table 4. The EFG of As in LaFeAsO within NM, FM and Q_M AFM states at different doping levels, calculated by WIEN2k using the PBE(GGA) XC functional. The unit is 10^{21} V m^{-2} .

As doping	V_{xx}			V_{yy}		
	Up	Dn	Total	Up	Dn	Total
NM Undoped	0.69	0.69	1.38	0.69	0.69	1.38
0.1h (La)	0.70	0.70	1.40	0.70	0.70	1.40
0.1e (La)	0.65	0.65	1.31	0.65	0.65	1.31
0.1e (O)	0.66	0.66	1.32	0.66	0.66	1.32
FM Undoped	0.55	0.81	1.36	0.55	0.81	1.36
0.1h (La)	0.58	0.68	1.26	0.58	0.68	1.26
0.1e (La)	0.56	0.74	1.30	0.56	0.74	1.30
0.1e (O)	0.58	0.75	1.23	0.58	0.75	1.23
Q_M Undoped	-0.40	-0.40	-0.80	0.77	0.77	1.54
0.1h (La)	-0.42	-0.42	-0.84	0.68	0.68	1.36
0.1e (La)	-0.41	-0.41	-0.82	0.89	0.89	1.78
0.1e (O)	-0.40	-0.40	-0.80	0.91	0.91	1.82
0.2e (O)	-0.29	-0.29	-0.58	1.03	1.03	2.06

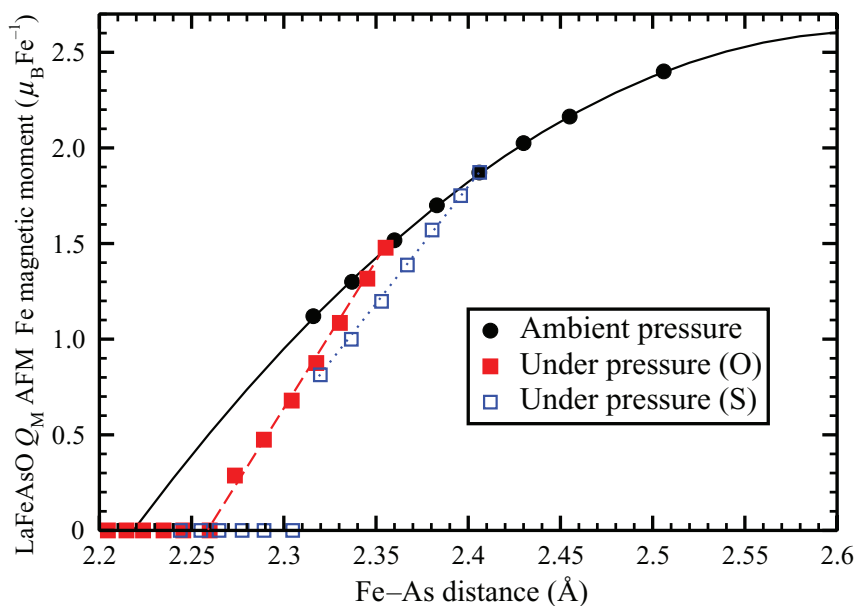


Figure 6. Plot of the magnetic moment of Fe atom in the Q_M AFM state of LaFeAsO as a function of the Fe–As distance, both at ambient pressure and under pressure.

i.e. we consider only the $(\pi\pi 0)$ order. We have performed a relaxation (shape of the cell as well as atom positions) of LaFeAsO for different volumes, the results being presented in figure 10. The calculated equilibrium lattice parameters as well as the internal atomic positions are reported in table 5, together with available experimental data. The overall agreement is

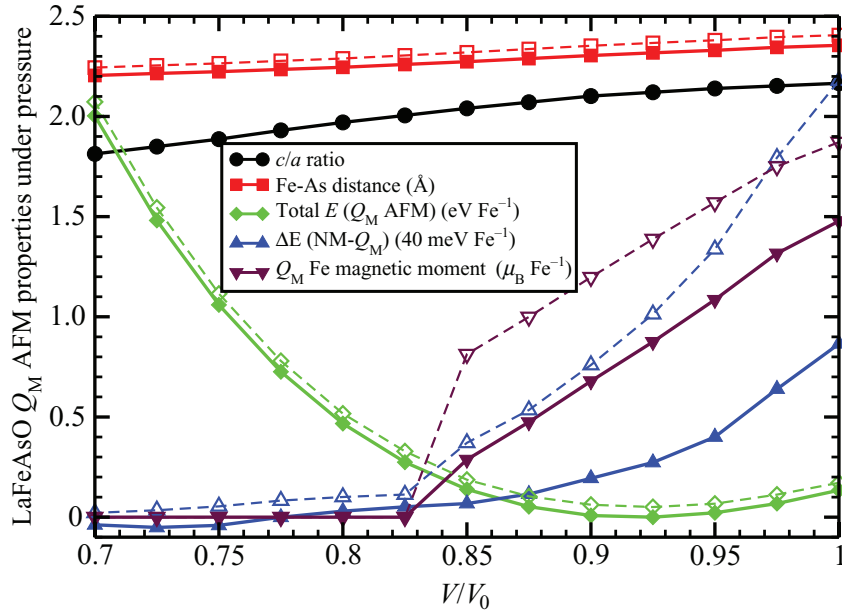


Figure 7. Plot of the optimized c/a ratio, the Fe–As distances (\AA), the total energy of the Q_M AFM state (eV Fe^{-1}), the total energy differences between NM and Q_M AFM state ($EE(\text{NM})-EE(Q_M \text{ AFM})$) (40 meV Fe^{-1}), the magnetic moment (μ_B) of the Q_M AFM states as a function of V/V_0 . Curves with solid lines, filled symbols are for the optimized $z(\text{As})$ while curves with dash lines, empty symbols are for the shifted $z(\text{As})$.

satisfactory, the length of the a and b lattice cell vectors being slightly overestimated by our calculations, whereas the value of c is slightly underestimated. The value of $|\delta|$ (the monoclinic distortion angle) is overestimated by our calculations, but the very small distortion and very small energy difference makes this difference understandable. The important point is that *ab-initio* calculations are indeed able to reproduce the structural instability of LaFeAsO.

As for the atom positions within the cell, the agreement is good for the positions of La, O and Fe but is less satisfying for the internal position $z(\text{As})$ of arsenic. The difficulty concerning the position of As has been reported by us previously [18] and is related to the strong magnetophonon coupling that occurs in this compound. In figure 10, we present the corresponding lattice parameters (upper plot), magnetic moment (middle plot), and internal coordinate of As (z_{As}) (lower plot), versus volume for LaFeAsO. The range of pressure covered goes roughly from -2.5 GPa to 2.5 GPa. By fitting the $E-V$ data (not shown here) to a Birch–Murnaghan equation of state (EOS), we find LaFeAsO to have a bulk modulus of $B_0 = 75$ GPa and a bulk modulus derivative $B'_0 = 4.1$. Also, from the upper plot of figure 10, we predict that LaFeAsO is more compressible along the c -axis than along the a and b axes, a common characteristic of this type of layered material.

More important is the dependence of the magnetic moment on the volume (middle plot of figure 10). This dependence has two origins: the first one is the usual dependence of the magnetic moments on the volume change, but in LaFeAsO, the magnetic moment on Fe is known [18] to be strongly dependent on the internal coordinate of As which changes with applied pressure (lower plot of figure 10).

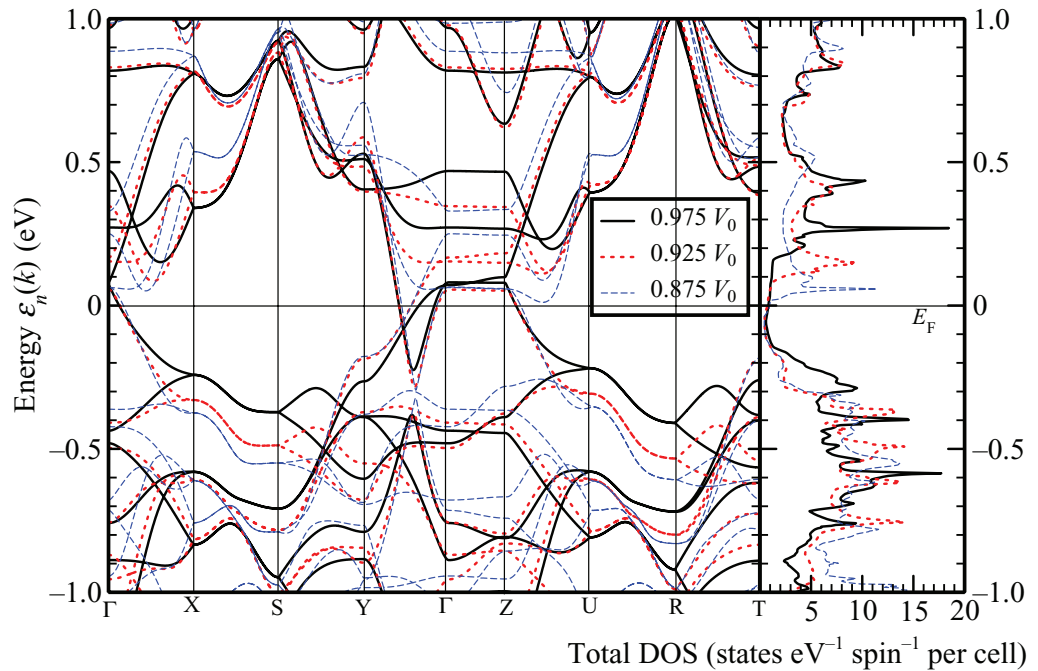


Figure 8. The band structure and total DOS of Q_M LaFeAsO computed for $0.975V_0$, $0.925V_0$ and $0.875V_0$. $z(\text{As})$ has been shifted.

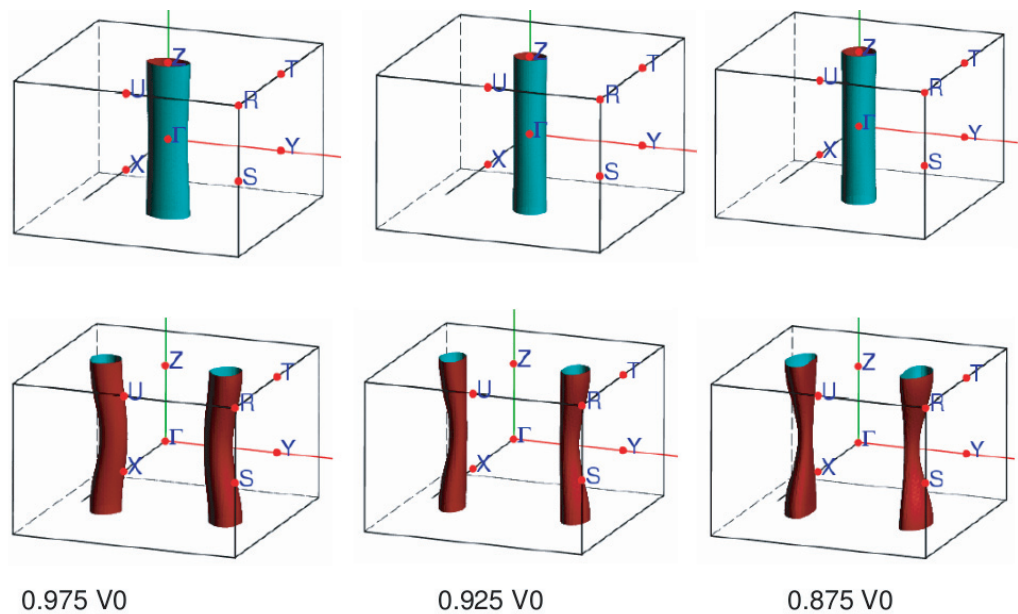


Figure 9. The Fermi surface of Q_M LaFeAsO computed for $0.975V_0$, $0.925V_0$ and $0.875V_0$. $z(\text{As})$ has been shifted.

The structural distortion has been addressed by Yildirim [40, 55], who approached the question differently and obtained different results. While our value of the Fe moment is close to that for the undistorted structure as would be expected, the moment reported by Yildirim is $0.48 \mu_B$ per Fe atom. We checked carefully the possible existence of such a magnetic solution,

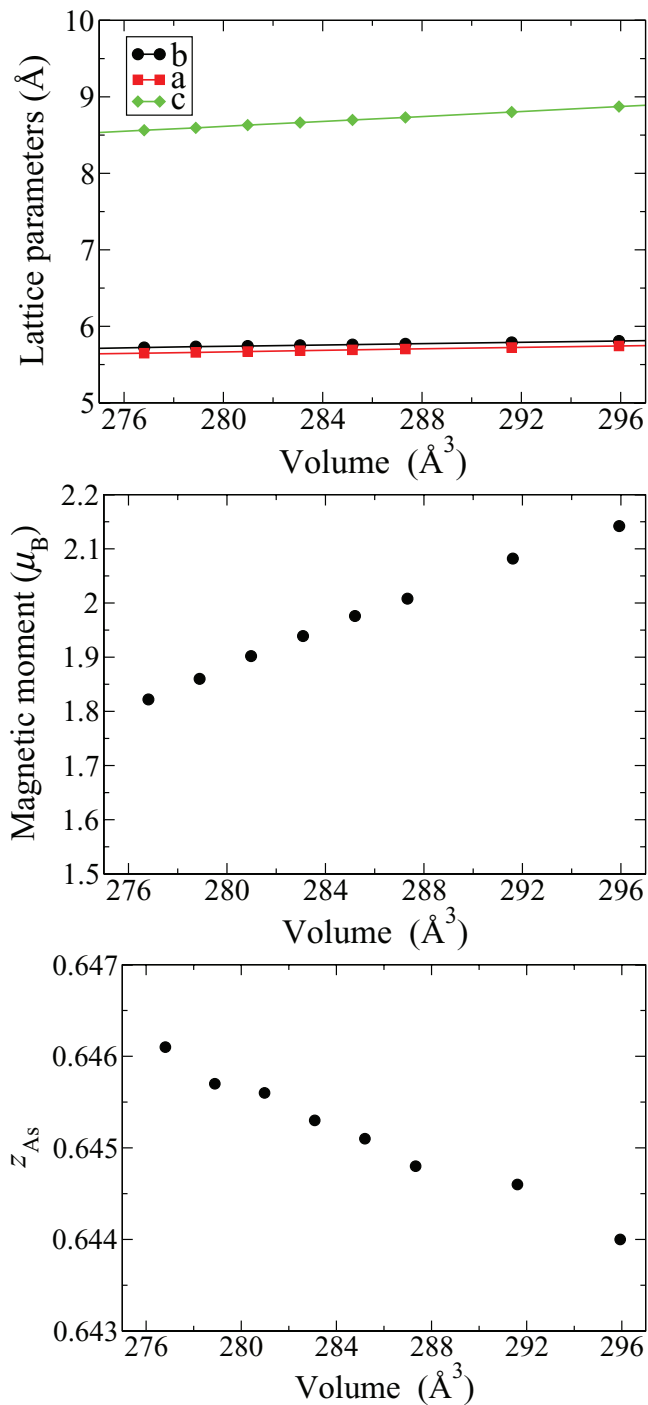


Figure 10. Upper plot: lattice parameters versus volume. Middle plot: magnetic moment versus volume. Lower plot: z_{As} versus volume.

but our calculations appears to be robust, with the magnetic moment of Fe being around $2 \mu_B$. As a result of the different magnetic moment, his computed DOS (see figure 5 in [40]) also is different. Together with an experimental study, Nomura *et al* [8] reported *ab-initio* calculations on LaFeAsO for both the tetragonal and orthorhombic structures, and found almost vanishing

Table 5. Left and middle columns: the structure parameters of LaFeAsO in its low-temperature phase as obtained from x-ray [8] and neutron [7] studies, as reported by Yildirim [55]. Right column: results from calculations obtained after a full relaxation of a $\sqrt{2} \times \sqrt{2}$ cell with a $(\pi, \pi, 0)$ magnetic order. a , b and c are the lattice parameters, $|\delta|$ is the monoclinic distortion angle of the primitive cell, and $\text{La}(z)$, $\text{As}(z)$, $\text{O}(z)$ and $\text{Fe}(z)$ are the internal coordinates of the corresponding atom.

	X-ray (120 K)		Neutron (4 K)	Calculations
	$\sqrt{2} \times \sqrt{2}$	Primitive	Primitive	$\sqrt{2} \times \sqrt{2}$
a	5.682 62 Å	4.028 06 Å	4.0275 Å	5.69 Å
b	5.710 43 Å	4.028 06 Å	4.0275 Å	5.76 Å
c	8.719 64 Å	8.719 64 Å	8.7262 Å	8.70 Å
$ \delta $		0.2797°	0.279°	0.69°
$\text{La}(z)$		0.141 71	0.1426	0.1418
$\text{As}(z)$		0.651 29	0.6499	0.6451
$\text{O}(z)$		0	-0.0057	0.0
$\text{Fe}(z)$		0.5	0.5006	0.5

magnetic moments, which correspond to a non-magnetic ground state. In our case, such a state is higher in energy by about 140 meV per Fe atom for the fully relaxed structure, and therefore can safely be ruled out as being the true ground state of LaFeAsO. The differences in calculated values that we have noted reflect an unusual sensitivity to details (structure, method and XC functional).

5.2. (π, π, π) magnetic order

We turn now to the investigation of LaFeAsO taking into account both the true (π, π, π) magnetic order and the structural distortion. In this case, we have used the experimental structural data provided by de la Cruz *et al* [7]. As in the case of the $(\pi, \pi, 0)$ order, there are two possible magnetically ordered states. Only one gives the (π, π, π) order to be the ground state versus the $(\pi, \pi, 0)$ order, and by only a few meV per Fe atom. This small energy difference is near the limit of precision of our calculations, but appears to confirm the sign of the very weak magnetic interaction along the c layers.

The corresponding band structure is shown in figure 11. Due to the doubling of the cell along the c -axis, there are now four bands crossing the Fermi level (see figure 3 of [18]). Along S–Y there are tiny splittings around -0.25 and -0.6 eV as well as along Γ –X and Γ –Y, indicating the magnitude of interlayer coupling. In particular, the splitting is particularly large for one pair of bands just above E_F at Γ . Along the zone boundary X–S–Y, the bands nearest the Fermi level are hardly split at all. Overall, the band structure retains the essential features noticed before [18], namely a pseudogap separating bonding and antibonding states over much of the zone, together with dispersive bands crossing the Fermi level along only one of the two in-plane directions (Γ –X, with our choice of axes).

The total and partial densities of states are very similar to the ones in the case of a $(\pi, \pi, 0)$ magnetic order and will not be shown here; but we notice that the rough electron/hole symmetry

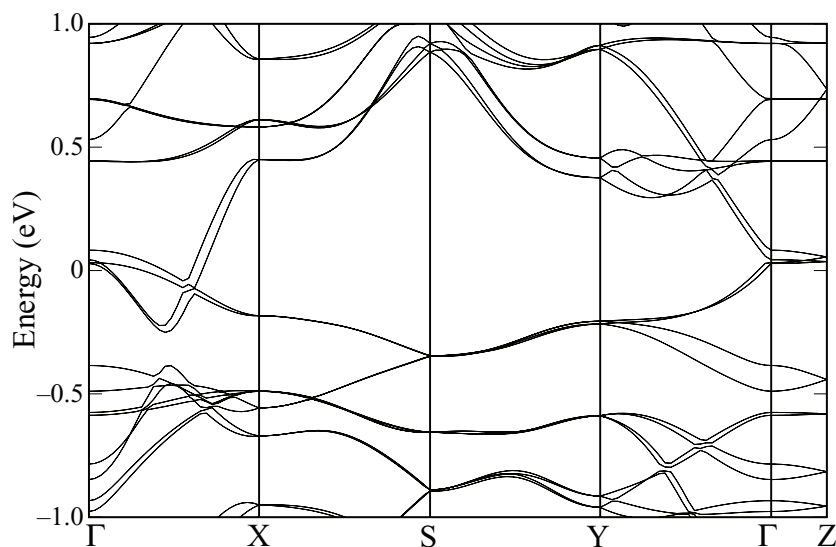


Figure 11. The bandstructure of LaFeAsO along high symmetry directions in the case of a (π, π, π) magnetic order for the distorted (orthorhombic) $\sqrt{2} \times \sqrt{2} \times 2$ cell. The high symmetry points are defined as $\Gamma(0, 0, 0)$; $X(0.5, 0, 0)$; $S(0.5, 0.5, 0)$; $Y(0, 0.5, 0)$ and $Z(0, 0, 0.5)$, in terms of reciprocal lattice vectors.

in view of the study of doped (superconducting) materials is preserved. Also, our calculated Fermi surface (not shown here), made of four sheets, is very similar to the one presented previously [18] for the $(\pi, \pi, 0)$ order and folded back along k_z : it has two sheets along the Γ – Z direction which are almost perfectly cylindrical, while the two other sheets are more distorted, but still showing a strong two-dimensional character.

6. Role of the pnictogen atom

As mentioned at the beginning of section 1 of this paper, LaFeAsO and LaFePO are isostructural and isovalent, but they have quite different properties: LaFeAsO is Q_M AFM ordered below $T_N = 150$ K, while LaFePO shows no magnetic order. Also, they have completely different response to doping: either electron or hole doping will destroy the Q_M AFM ordering in LaFeAsO and make it superconducting with T_c over 26 K [9] (43 K under pressure [19]), while in LaFePO, superconductivity is reported only up to 9 K [1]. A deeper understanding of the differences of the electronic structure of these two compounds can provide insight into the competition between magnetic ordering and superconductivity. For similar reasons, the related compounds LaFeNO and LaFeSbO (although not studied experimentally yet) are potentially of high interest, so we also provide predictions for their electronic structure.

Table 6 displays the experimental structure parameters for LaFePO [1] and LaFeAsO [9] as well as the predicted structure for LaFeNO and LaFeSbO after optimization (see below for calculation details). If not specified, properties reported in this section are calculated using the structure parameters listed in table 6. As a result of the increasing size of the pnictogen atom, the Fe–Pn length changes. In particular, the Fe–Pn distance is consistent with the sum of the covalent radii of Fe and Pn, which reflects the covalent bonding nature between Fe and Pn

Table 6. Structural parameters of LaFePnO (Pn = N, P, As or Sb), as obtained experimentally for LaFePO [1] and LaFeAsO [9] or from our calculations for LaFeNO and LaFeSbO. Length units are in Å, $z(\text{La})$ and $z(\text{Pn})$ are the internal coordinate of the lanthanum atom and the pnictide atom, and ‘Sum’ means the sum of Fe covalent radius and the Pn covalent radius, which is quite close to the calculated value in all cases.

Pn	a (Å)	c (Å)	c/a	$z(\text{La})$	$z(\text{Pn})$	La–O	Fe–Pn	Sum
N	3.6951	8.0802	2.187	0.170	0.609	2.302	2.047	2.00
P	3.9636	8.5122	2.148	0.149	0.634	2.352	2.286	2.31
As	4.0355	8.7393	2.166	0.142	0.651	2.369	2.411	2.44
Sb	4.1626	9.3471	2.246	0.127	0.671	2.396	2.624	2.62

Table 7. Calculated magnetic moment of Fe, and total energy relative to the NM (FM) states of Q_0 AFM, and Q_M AFM states of LaFePnO from FPLO7 with PW92 XC functional. Lattice parameters that were used are listed in table 4.

Pn	Magnetic moment (μ_B)			$\Delta E E$ (meV Fe $^{-1}$)	
	Q_M	Q_0	FM	FM– Q_M	Q_0 – Q_M
N	1.63	0.80	0.027	41.0	40.0
P	0.56	—	0.087	1.6	—
As	1.87	1.72	0.002	87.2	62.6
Sb	2.47	2.43	0.000	293.8	82.4

atoms in this family. The slight increase of the La–O distance through the series is just a size effect related to the expansion of the volume.

The values of the Fe magnetic moment for LaFePnO with FM/NM, Q_0 AFM, Q_M AFM states, and their total energy differences are presented in table 7. Apart from LaFePO, all the members of the LaFePnO family studied here have a large Fe magnetic moment in the Q_M AFM state, the corresponding total energy being significantly lower than the ones corresponding to FM/NM state.

6.1. LaFePO

LaFePO was the first member of the iron oxypnictide family to be reported to be superconducting [1]. The corresponding electronic structure was studied by Lebègue using *ab-initio* calculations [14], but considering only a non-magnetic ground state. Since then LaFePO has been studied using various experimental tools. From photoemission spectra [56]–[58], it was concluded that the Fe 3d electrons are itinerant, and that there is no pseudogap in LaFePO. Magnetic measurements revealed [5, 59] that LaFePO is a paramagnet, while electron-loss spectroscopy [60] implied a significant La–P hybridization. The absence of long-range order in LaFePO was confirmed by Mössbauer spectroscopy [3] and it was proposed that LaFePO and doped LaFeAsO could have different mechanisms to drive the superconductivity in these compounds. Also, further theoretical studies were performed [58]–[60] but without studying all the possible magnetic states.

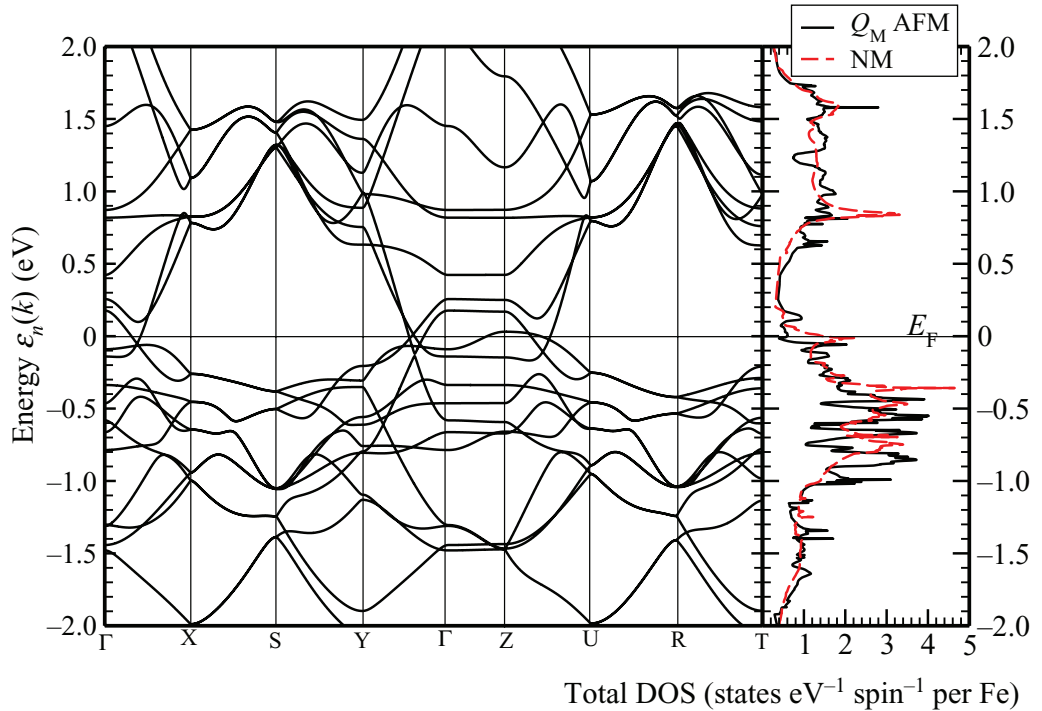


Figure 12. Plot of LaFePO band structure in Q_M AFM state and total DOS in both Q_M AFM and NM states at ambient conditions with experimental lattice parameters.

In our calculations (performed with the lattice parameters reported in [1]), we find that for FM order Fe has a weak magnetic moment of about $0.09 \mu_B$, with a total energy very close to the NM one; this result is much like what is found in LaFeAsO. A remarkable difference is that the Q_0 AFM state cannot be obtained. However, we found the Q_M AFM state to be the lowest in energy, but only by about 1.6 meV Fe^{-1} , which is about two orders of magnitude less than in LaFeAsO. LaFePO, therefore, presents the situation where all of the three possible magnetic states are all very close in energy to the nonmagnetic state, in contrast with LaFeAsO for which the Q_M AFM order was clearly the ground state. Thus LaFePO seems to be near magnetic quantum criticality.

The band structure of Q_M AFM LaFePO is displayed in figure 12 together with total DOS for both Q_M AFM and NM states. This band structure is quite different from that of LaFeAsO with the same Q_M order, with the most significant differences along Γ -X, Γ -Y and Γ -Z lines. The difference is because the breaking of the x - y symmetry is much smaller in the Q_M AFM LaFePO compared with LaFeAsO, because the calculated Fe moment is only $0.56 \mu_B$ in LaFePO (it is $1.87 \mu_B$ in LaFeAsO with the same calculational method). The corresponding DOS is also different from that of LaFeAsO: there is structure within the pseudogap around Fermi level in LaFePO (see figure 12). The difference in total DOS at E_F is significant: it is only $0.2 \text{ states eV}^{-1} \text{ spin}^{-1} \text{ per Fe}$ for LaFeAsO, but it is $0.6 \text{ states eV}^{-1} \text{ spin}^{-1} \text{ per Fe}$ for LaFePO. In the NM state of LaFePO, it is even larger with $1.6 \text{ states eV}^{-1} \text{ spin}^{-1} \text{ per Fe}$. The DOS of Q_M AFM LaFePO is fairly flat from the Fermi level (set to 0.0 eV) to 0.6 eV , so that electron doping of LaFePO will increase the Fermi level, but will hardly change $N(E_F)$ (in a rigid band picture).

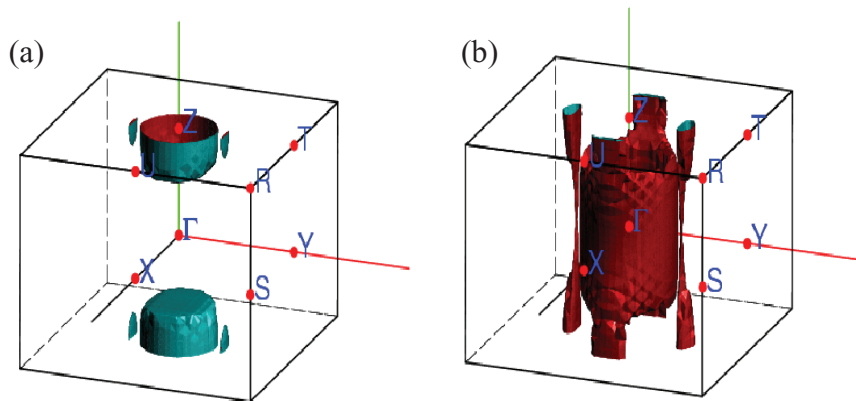


Figure 13. Fermi surface of Q_M AFM LaFePO, showing the very strong differences compared with LaFeAsO.

An important consequence is that there will be no expected enhancement of T_C coming from $N(E_F)$ upon electron doping. In order to see a significant increase of $N(E_F)$ in Q_M AFM LaFePO, an electron doping level of at least $1.2 e^- Fe^{-1}$ is required, which seems unrealistically large based on the existing doping studies in these materials. This conclusion remains valid in the case of NM LaFePO, since apart from a peak around Fermi level, the DOS is about the same as for the Q_M AFM state. Again, the behavior is quite different from that of Q_M AFM LaFeAsO: $0.1 e^- Fe^{-1}$ doping will increase its $N(E_F)$ by a factor of 6: from 0.2 states $eV^{-1} spin^{-1}$ per Fe to 1.2 states $eV^{-1} spin^{-1}$ per Fe.

The Fermi surface of Q_M AFM LaFePO is shown in figure 13. Compared to the Fermi surface of Q_M AFM LaFeAsO presented earlier by Yin *et al* [18], the piece enclosing the Γ -Z line (containing holes) increases in size and its x - y cross section becomes more circular rather than elliptic. There is another piece (absent in LaFeAsO) also enclosing the Γ -Z line with the same shape but larger in size and containing electrons instead of holes. The two symmetric electron-type pieces of Fermi surface lying along the Γ -Y direction in LaFeAsO reduce in size in LaFePO, but it has two additional similar pieces lying along the Γ -X direction. LaFePO has one more hole-type Fermi surface cylinder surrounding the Z point. This Fermi surface is, understandably, quite different from the Fermi surface of NM LaFePO presented earlier [14].

Therefore, while they are isostructural and isovalent, and have similar covalence, LaFePO and LaFeAsO present important differences in their respective electronic structures. These differences must form the underpinning of any explanation of why doped LaFePO and LaFeAsO have such different critical temperatures.

6.2. LaFeSbO

Since the experimental crystal structure of LaFeSbO is not reported yet, we conducted calculations to obtain the structure. The procedure we used is the following: starting from the experimental volume V_0 of LaFeAsO (but with As replaced by Sb), we first optimized c/a , $z(\text{La})$ and $z(\text{Sb})$. Then we chose a higher volume and again optimized the parameters, finally finding the volume that has the lowest total energy. Using this scheme, the optimized volume is $1.046V_0$, whereas for LaFeAsO the equilibrium volume is about $0.919V_0$. Assuming that PW92 overbinds equally for LaFeSbO as for LaFeAsO, the experimental equilibrium volume for

Table 8. Optimized structure parameters for LaFeSbO at several volumes. The accuracy for c/a is within 0.3%, and within 0.8% for $z(\text{La})$ and $z(\text{Sb})$.

V/V_0	a (Å)	c (Å)	c/a	$z(\text{La})$	$z(\text{Sb})$
1.000	4.092	8.500	2.077	0.137	0.665
1.050	4.118	8.812	2.140	0.133	0.663
1.100	4.141	9.131	2.205	0.129	0.661
1.125	4.155	9.274	2.232	0.128	0.660
1.138	4.163	9.347	2.245	0.127	0.660
1.150	4.169	9.418	2.259	0.126	0.659

LaFeSbO should be $1.046/0.919 = 1.138V_0$. Finally, we performed calculations for a range of volume from $V = V_0$ to $V = 1.150V_0$, the corresponding structural parameters being presented in table 8.

Since for LaFeAsO in the Q_M AFM phase PW92 underestimated $z(\text{As})$ by 0.011 at its experimental volume, we corrected $z(\text{Sb})$ by adding 0.011 to the optimized $z(\text{Sb})$ (we refer to this position at the ‘shifted $z(\text{Sb})$ ’). Both for the NM and Q_M AFM case, there are only small differences near E_F between the optimized $z(\text{As})$ and shifted $z(\text{As})$ in the band structure and DOS, as seen in figure 14. However, shifting $z(\text{Sb})$ induces important changes in the energy differences between NM and Q_M AFM states, which are provided in table 9. Also, the magnetic moment of Fe, and the energy differences among NM/FM, Q_0 AFM and Q_M AFM are strongly dependent on volume. With decreasing volume, the difference in energy between the different magnetic states decreases quickly.

At $1.138V_0$, which is the inferred equilibrium volume of LaFeSbO, the properties of NM/FM, Q_0 AFM and Q_M AFM are very similar to the ones of LaFeAsO at its experimental volume. Thus from these results we expect that doped LaFeSbO should have properties similar to those of LaFeAsO.

6.3. LaFeNO

The structure of LaFeNO is also not reported experimentally. In order to obtain it, the same procedure as for LaFeSbO was used. The lowest total energy is at $0.762V'_0$ (here V'_0 is the experimental volume of LaFePO). Again assuming PW92 makes a similar error as it makes in LaFeAsO, we predict its equilibrium volume to be close to $0.825V'_0$. At $0.825V'_0$ and for larger volume, the total energy of the Q_M AFM state is well below that of the FM/NM state (see table 10). Therefore, LaFeNO, if it can be synthesized, should have the Q_M AFM ordered state at low temperature, similar to LaFeAsO and our prediction of LaFeSbO.

Compared with the other LaFePnO compounds, LaFeNO is even closer to being a semimetal when the volume is equal to $0.825V'_0$, and it becomes a small gap insulator at $0.850V'_0$ and a higher carrier density metal at $0.800V'_0$ (see figure 15). The DOS for $0.825V'_0$ shows a pseudogap around E_F , but the DOS is somewhat less flat than it is for LaFeAsO.

When LaFeNO is calculated to be insulating (for volumes larger than $0.825V'_0$), the gap can be taken to *define* a distinction between bonding (occupied) and antibonding (unoccupied) states. The appearance of this gap in LaFeNO is quite surprising: although there is clear separation of valence and conduction bands over most of the zones for LaFeAsO, there is no

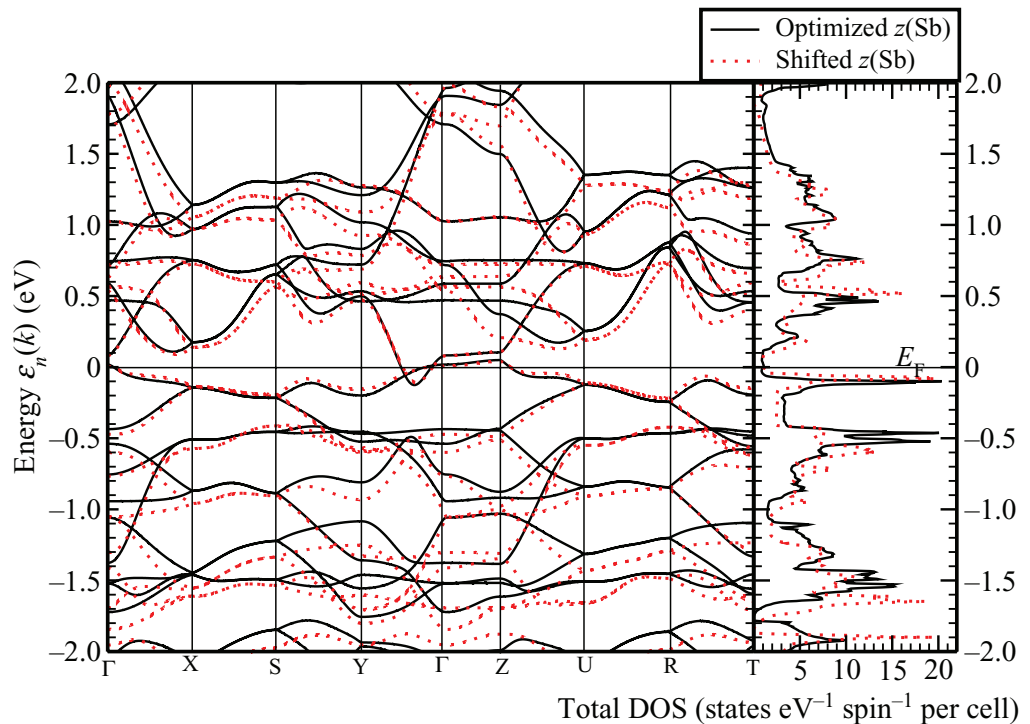


Figure 14. Plot of Q_M AFM LaFeSbO band structure and total DOS at $1.138V_0$ with both optimized and shifted $z(\text{Sb})$.

way to ascribe the small FSs to simple overlapping valence and conduction bands: in LaFeAsO and LaFeSbO, the bonding and antibonding bands are never completely separated from each other. In LaFeNO this separation finally becomes apparent, as an actual bandgap does appear.

7. Role of the rare earth atom in ReFeOAs

Since LaFeAsO was discovered, after appropriate variation of the carrier concentration, to be superconducting at 26 K, much substitution on the rare earth (R) site has been done, with impressive increases in the critical temperature. Since all members are trivalent, it becomes important to uncover the influence of the Re atom: is it some aspect of the chemistry, which does differ among the rare earths? Is it an effect of size? Or can there be some other subtle effect?

Table 11 is a collection of the lattice constants a and c , volume V of the primitive cell, and T_c onset of ReFeOAs reported from experiment [61]–[64]. Both lattice constants, hence the volume, decrease monotonically as the atomic number increases, but T_c increases only from La to Gd, whereupon it drops for heavier rare earths. Since we have found that small details affect the electronic and magnetic structure—especially $z(\text{As})$ —it is important to assess the size effect. We have performed calculations on Ce, Nd and Gd, using LSDA + U with $U = 7.0$ eV and $J = 1$ eV applied to the Re atom to occupy the 4f shell appropriately and keep the 4f states away from the Fermi level. These compounds all have DOS and band structures very similar to those of LaFeAsO. To investigate further, we checked GdOFeAs using the crystal structure of LaFeAsO. The resulting band structure and DOS are almost identical to the original results for

Table 9. Calculated magnetic moment of Fe, total energy relative to the NM (FM) states of Q_0 AFM and Q_M AFM with the optimized structure of LaFeSbO at several volumes from FPLO7 with PW92 XC functional. Upper part: $z(\text{Sb})$ is optimized. Lower part: $z(\text{Sb})$ is optimized and shifted.

V/V_0	Magnetic moment (μ_B)			ΔEE (meV Fe^{-1})	
	Q_M	Q_0	FM	FM- Q_M	Q_0 - Q_M
1.000	1.58	1.12	0.36	60.1	60.1
1.050	1.87	1.74	0.44	95.6	68.0
1.100	2.09	2.00	0.00	147.6	70.7
1.125	2.17	2.10	0.00	172.6	71.8
1.138	2.23	2.16	0.00	190.6	72.5
1.150	2.26	2.19	0.00	199.0	72.0
1.050	2.17	2.08	0.72	158.1	78.0
1.100	2.35	2.00	0.00	223.8	80.8
1.125	2.42	2.37	0.00	271.6	81.8
1.138	2.47	2.42	0.00	293.8	82.4
1.150	2.49	2.45	0.00	287.6	82.1

Table 10. Calculated magnetic moment of Fe in LaFeNO, total energy relative to the NM (FM) states of Q_0 AFM and Q_M AFM with the optimized structure at several volumes, but with $z(N)$ shifted up by 0.011, as a compensation of what PW92 does to LaFeAsO, where PW92 underestimates $z(\text{As})$ by 0.011.

V/V'_0	Magnetic moment (μ_B)			ΔEE (meV Fe^{-1})	
	Q_M	Q_0	NM/FM	NM/FM- Q_M	Q_0 - Q_M
0.900	2.21	1.69	1.64	209.8	135.9
0.875	2.06	1.51	0.03	114.9	99.2
0.850	1.88	1.14	0.03	74.3	68.1
0.825	1.63	0.80	0.03	41.0	40.0
0.800	1.26	–	0.00	18.4	–
0.787	1.08	–	0.00	11.3	–
0.775	0.90	–	0.00	7.0	–
0.762	0.00	–	0.00	1.3	–
0.750	0.00	–	0.00	1.4	–
0.725	0.00	–	0.00	1.2	–
0.700	0.00	–	0.00	0.9	–

Gd, thus there seems to be no appreciable effect of the differing chemistries of Gd and La. This negative result supports the idea that the size difference may be dominant. The difference in size (hence a , c and the internal coordinates) influences not only the band structure and DOS, but also the magnetic properties. Fixed spin moment calculations in the FM state give the lowest total energy at $0.2 \mu_B \text{Fe}^{-1}$ in LaFeAsO and $0.5 \mu_B \text{Fe}^{-1}$ in both GdOFeAs and La-replaced GdOFeAs.

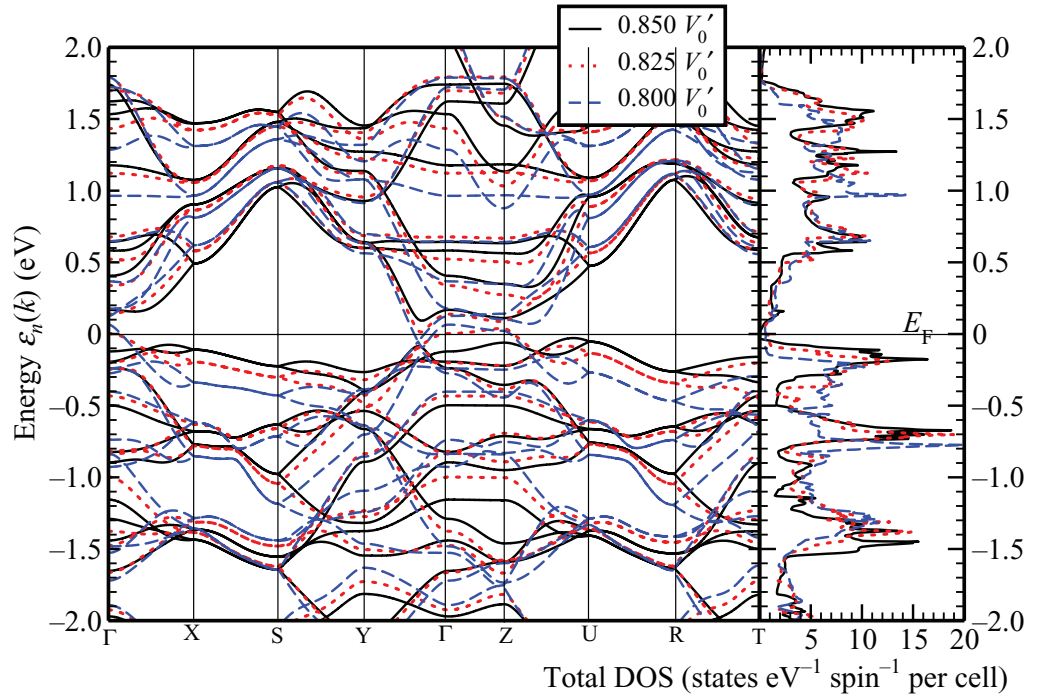


Figure 15. Plot of LaFeNO Q_M AFM band structure and total DOS at $0.850V'_0$, $0.825V'_0$ and $0.800V'_0$ with shifted $z(N)$.

Table 11. Collection of the lattice constants a (Å) and c (Å), volume V (Å³) of the primitive cell, and the onset temperature T_c (K), of RFeOAs (R) reported from experiments.

Element	Z	a (Å)	c (Å)	V (Å ³)	$T_{C,onset}$ (K)
La	57	4.033	8.739	142.14	31.2
Ce	58	3.998	8.652	138.29	46.5
Pr	59	3.985	8.595	136.49	51.3
Nd	60	3.965	8.572	134.76	53.5
Sm	62	3.933	8.495	131.40	55.0
Gd	64	3.915	8.447	129.47	56.3
Tb	65	3.899	8.403	127.74	52
Dy	66	3.843	8.284	122.30	45.3

8. Summary

We have investigated in some detail the electronic structure and magnetic properties of the LaFeAsO class of novel superconductors using *ab-initio* methods. The effects of the Fe–As distance, of doping, and of pressure, as well as calculations of the EFGs have been reported. Approximate electron–hole symmetry versus doping is found, which is also seen in experiment, and strong magnetophonon coupling is observed. These two seem to be primary characteristics of the LaFeAsO system, and are ingredients that need to be understood to proceed with the study of the mechanism of superconducting pairing. We calculated effects of the structural distortion and of the true (π, π, π) magnetic order, as well as with the $(\pi, \pi, 0)$ simplification that is

often used, finding that experiments can be reproduced fairly well by our calculations. Finally, the related materials LaFePO, LaFeSbO and LaFeNO were investigated and their properties compared to those of LaFeAsO. From these comparisons, it appears that LaFePO is significantly different from the other materials studied here. Also, in view of their similarities with LaFeAsO, doped LaFeSbO and LaFeNO are potential candidates as superconductors.

Acknowledgments

We acknowledge financial support from ANR PNANO grant nos ANR-06-NANO-053-02 and ANR-BLAN07-1-186138 (SL) and from DOE grant DE-FG02-04ER46111 (WEP). WEP is happy to acknowledge a grant from the France Berkeley Fund that enabled the initiation of this project.

References

- [1] Kamihara Y, Hiramatsu H, Hirano M, Kawamura R, Yanagi H, Kamiya T and Hosono H 2006 *J. Am. Chem. Soc.* **128** 10012
- [2] Liang C Y *et al* 2007 *Supercond. Sci. Technol.* **20** 687
- [3] Tegel M, Schellenberg I, Pottgen R and Johrendt D 2008 *Z. Naturforsch. B* **63b** 1057–61
- [4] Hamlin J J, Baumbach R E, Zocco D A, Sayles T A and Maple M B 2008 *J. Phys.: Condens. Matter* **20** 365220
- [5] McQueen T M, Regulacio M, Williams A J, Huang Q, Lynn J W, Hor Y S, West D V, Green M A and Cava R J 2008 *Phys. Rev. B* **78** 024521
- [6] Analytis J G, Chu J-H, Erickson A S, Kucharczyk C, Serafin A, Carrington A, Cox C, Kuzlarich S M, Hope H and Fisher I R 2008 arXiv:0810.5368
- [7] de la Cruz C, Huang Q, Lynn J W, Li J, Ratcliff II W, Zarestky J L, Mook H A, Chen G F, Luo J L, Wang N L and Dai P 2008 *Nature* **453** 899
- [8] Nomura T, Kim S W, Kamihara Y, Hirano M, Sushko P V, Kato K, Takata M, Shluger A L and Hosono H 2008 *Supercond. Sci. Technol.* **21** 125028
- [9] Kamihara Y, Watanabe T, Hirano M and Hosono H 2008 *J. Am. Chem. Soc.* **130** 3296
- [10] Rotter M, Pangerl M, Tegel M and Johrendt D 2008 *Angew. Chem., Int. Edn. Engl.* **47** 7949–52
- [11] Alireza P L, Gillett J, Ko Y T C, Sebastian S E and Lonzarich G G 2009 *J. Phys.: Condens. Matter* at press (arXiv:0807.1896)
- [12] Kotegawa H, Sugawara H and Tou H 2009 *J. Phys. Soc. Japan* **78** at press (arXiv:0810.4856)
- [13] Ren Z-A *et al* 2008 *Chin. Phys. Lett.* **25** 2215–6
- [14] Lebègue S 2007 *Phys. Rev. B* **75** 035110
- [15] Singh D J and Du M-H 2008 *Phys. Rev. Lett.* **100** 237003
- [16] Kurmaev E Z, Wilks R G, Moewes A, Skorikov N A, Izyumov Yu A, Finkelstein L D, Li R H and Chen X H 2008 arXiv:0805.0668
- [17] Luetkens H *et al* 2008 arXiv:0806.3533
- [18] Yin Z P, Lebègue S, Han M J, Neal B P, Savrasov S Y and Pickett W E 2008 *Phys. Rev. Lett.* **101** 047001
- [19] Takahashi H, Igawa K, Arii K, Kamihara Y, Hirano M and Hosono H 2008 *Nature* **453** 376
- [20] Lu W, Yang J, Dong X L, Ren Z A, Che G C and Zhao Z X 2008 *New J. Phys.* **10** 063026
- [21] Zimmer B I, Jeitschko W, Albering J H, Glaum R and Reehuis M 1995 *J. Alloys Compd.* **229** 238
- [22] Quebe P, Terbuchte L J and Jeitschko W 2000 *J. Alloys Compd.* **302** 70
- [23] Hohenberg P and Kohn W 1964 *Phys. Rev.* **136** B864
- [24] Kohn W and Sham L 1965 *Phys. Rev.* **140** A1133
- [25] Koepernik K and Eschrig H 1999 *Phys. Rev. B* **59** 1743
- [26] Koepernik K, Velicky B, Hayn R and Eschrig H 1997 *Phys. Rev. B* **55** 5717

- [27] Blaha P, Schwarz K, Madsen G K H, Kvasnicka D and Luitz J 2001 WIEN2k, (K Schwarz, Technische Universität Wien, Austria)
- [28] Perdew J P and Wang Y 1992 *Phys. Rev. B* **45** 13244
- [29] Perdew J and Zunger A 1981 *Phys. Rev. B* **23** 5048
- [30] Perdew J, Burke K and Ernzerhof M 1996 *Phys. Rev. Lett.* **77** 3865
- [31] Perdew J P, Chevary J A, Vosko S H, Jackson K A, Pederson M R and Fiolhais C 1992 *Phys. Rev. B* **46** 6671
- [32] Blöchl P E 1994 *Phys. Rev. B* **50** 17953
- [33] Kresse G and Furthmüller J 1996 *Phys. Rev. B* **54** 11169
- [34] Kresse G and Joubert D 1999 *Phys. Rev. B* **59** 1758
- [35] Monkhorst H J and Pack J 1976 *Phys. Rev. B* **13** 5188
- [36] Blöchl P E, Jepsen O and Andersen O K 1994 *Phys. Rev. B* **49** 16223
- [37] Mazin I I, Singh D J, Johannes M D and Du M H 2008 *Phys. Rev. Lett.* **101** 057003
- [38] Ishibashi S, Terakura K and Hosono H 2008 *J. Phys. Soc. Japan* **77** 053709
- [39] Ma F, Lu Z-Y and Xiang T 2008 arXiv:0804.3370
- [40] Yildirim T 2008 *Phys. Rev. Lett.* **101** 057010
- [41] Boeri L, Dolgov O V and Golubov A A 2008 *Phys. Rev. Lett.* **101** 026403
- [42] Dong J *et al* 2008 *Europhys. Lett.* **83** 27006
- [43] Ma F and Lu Z-Y 2008 *Phys. Rev. B* **78** 033111
- [44] Xu G, Ming W, Yao Y, Dai X, Zhang S-C and Fang Z 2008 *Europhys. Lett.* **82** 67002
- [45] Cao C, Hirschfeld P J and Cheng H-P 2008 arXiv:0803.3236
- [46] Korotin M A, Streltsov S V, Shorikov A O and Anisimov V I 2008 arXiv:0805.3453
- [47] Vildosola V, Pourovskii L, Arita R, Biermann S and Georges A 2008 arXiv:0806.3285
- [48] Sushov P V, Shluger A L, Hirano M and Hosono H 2008 arXiv:0807.2213
- [49] Yildirim T 2008 arXiv:0807.3936
- [50] Mazin I I, Johannes M D, Boeri L, Koepfner K and Singh D J 2008 *Phys. Rev. B* **78** 085104
- [51] Grafe H-J, Paar D, Curro N J, Behr G, Werner J, Hamann-Borrero J, Hess C, Leps N, Klingeler R and Büchner B 2008 *Phys. Rev. Lett.* **101** 047003
- [52] Lorenz B, Sasmal K, Chaudhury R P, Chen X H, Liu R H, Wu T and Chu C W 2008 *Phys. Rev. B* **78** 012505
- [53] Fratini M, Caivano R, Puri A, Ricci A, Ren Z-A, Dong X-L, Yang J, Lu W, Zhao Z-X and Barba L 2008 *Supercond. Sci. Technol.* **21** 092002
- [54] McGuire M A, Christianson A D, Sefat A S, Sales B C, Lumsden M D, Jin R, Payzant E A, Mandrus D, Luan Y and Keppens V 2008 *Phys. Rev. B* **78** 094517
- [55] Yildirim T 2008 arXiv:0805.2888
- [56] Ishida Y, Shimojima T, Ishizaka K, Kiss T, Okawa M, Togashi T, Watanabe S, Wang X Y, Chen C T and Kamihara Y 2008 arXiv:0805.2647
- [57] Malaeb W, Yoshida T, Kataoka T, Fujimori A, Kubota M, Ono K, Usui H, Kuroki K, Arita R and Aoki H 2008 *J. Phys. Soc. Japan* **77** 093714
- [58] Lu D H, Yi M, Mo S K, Erickson A S, Analytis J, Chu J H, Singh D J, Hussain Z, Geballe T H and Fisher I R 2008 *Nature* **455** 81–84
- [59] Kamihara Y, Hirano M, Yanagi H, Kamiya T, Saitoh Y, Ikenaga E, Kobayashi K and Hosono H 2008 *Phys. Rev. B* **77** 214515
- [60] Che R, Xiao R, Liang C, Yang H, Ma C, Shi H and Li J 2008 *Phys. Rev. B* **77** 184518
- [61] Ren Z-A, Che G-C, Dong X-L, Yang J, Lu W, Yi W, Shen X-L, Li Z-C, Sun L-L and Zhou F 2008 *Europhys. Lett.* **83** 17002
- [62] Wang C, Li L, Chi S, Zhu Z, Ren Z, Li Y, Wang Y, Lin X, Luo Y and Jiang S 2008 *Europhys. Lett.* **83** 67006
- [63] Bos J-W G B, Penny G B S, Rodgers J A, Sokolov D A, Huxley A D and Attfield J P 2008 *Chem. Commun.* 3634–5
- [64] Li L, Li Y, Ren Z, Lin X, Luo Y, Zhu Z, He M, Xu X, Cao G and Xu Z 2008 *Phys. Rev. B* **78** 132506
- [65] Klauss H-H *et al* 2008 *Phys. Rev. Lett.* **101** 077005